

Package ‘dynamichazard’

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Type Package

Title Dynamic Hazard Models using State Space Models

Version 1.0.1

Description Contains functions that lets you fit dynamic hazard models using state space models. The first implemented model is described in Fahrmeir (1992) <[doi:10.1080/01621459.1992.10475232](https://doi.org/10.1080/01621459.1992.10475232)> and Fahrmeir (1994) <[doi:10.1093/biomet/81.2.317](https://doi.org/10.1093/biomet/81.2.317)>. Extensions hereof are available where the Extended Kalman filter is replaced by an unscented Kalman filter. See Christoffersen (2021) <[doi:10.18637/jss.v099.i07](https://doi.org/10.18637/jss.v099.i07)> for more details. Particle filters and smoothers are also supported more general state space models.

License GPL-2

LazyData TRUE

LinkingTo Rcpp, RcppArmadillo

Imports parallel, Rcpp (>= 0.12.6), boot

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BugReports <https://github.com/boennecd/dynamichazard/issues>

SystemRequirements C++11

URL <https://github.com/boennecd/dynamichazard>

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ddFixed	<i>Auxiliary Functions for Fixed Effects</i>
---------	--

Description

Functions used in formula of [ddhazard](#) for time-invariant effects. `ddFixed_intercept` is only used for the intercept.

Usage

```
ddFixed(object)

ddFixed_intercept(random_intercept = FALSE)
```

Arguments

`object` expression that would be used in formula. E.g. `x` or `poly(x, degree = 3)`.
`random_intercept` TRUE if a zero mean time-varying process should be included as an additional term. Only relevant in stationary models. See the `type` argument in [PF_EM](#).

Value

Returns the passed object.

Examples

```
# we can get a time-invariant effect of `x1` by
set.seed(1)
dat <- data.frame(stop = 1:20, event = rep(c(TRUE, FALSE), 10L), x1 = rnorm(20))
ddhazard(Surv(stop, event) ~ ddFixed(x1), dat,
         Q_0 = diag(1), by = 1, Q = diag(1))

# all of the calls below will yield the same result with a time-invariant
# intercept:
ddhazard(Surv(stop, event) ~ ddFixed_intercept() + x1, dat,
         Q_0 = diag(1), by = 1, Q = diag(1))
ddhazard(Surv(stop, event) ~ -1 + ddFixed_intercept() + x1, dat,
         Q_0 = diag(1), by = 1, Q = diag(1))
```

Description

Function to fit dynamic hazard models using state space models.

Usage

```
ddhazard(
  formula,
  data,
  model = "logit",
  by,
  max_T,
  id,
  a_0,
  Q_0,
  Q = Q_0,
  order = 1,
  weights,
  control = ddhazard_control(),
  verbose = FALSE
)
```

Arguments

formula	coxph like formula with <code>Surv(tstart, tstop, event)</code> on the left hand site of <code>~</code> .
data	<code>data.frame</code> or environment containing the outcome and covariates.
model	"logit", "cloglog", or "exponential" for respectively the logistic link function with discrete outcomes, the inverse cloglog link function with discrete outcomes, or for the continuous time model with piecewise constant exponentially distributed arrival times.
by	interval length of the bins in which parameters are fixed.
max_T	end of the last interval interval.
id	vector of ids for each row of the in the design matrix.
a_0	vector a_0 for the initial coefficient vector for the first iteration (optional). Default is estimates from static model (see static_glm).
Q_0	covariance matrix for the prior distribution.
Q	initial covariance matrix for the state equation.
order	order of the random walk.
weights	weights to use if e.g. a skewed sample is used.
control	list of control variables from ddhazard_control .
verbose	TRUE if you want status messages during execution.

Details

This function can be used to estimate survival models where the regression parameters follows a given order random walk. The order is specified by the `order` argument. 1. and 2. order random walks is implemented. The regression parameters are updated at time `by`, `2by`, ..., `max_T`. See the vignette("ddhazard", "dynamichazard") for details.

All filter methods needs a state covariance matrix Q_0 and state vector a_0 . An estimate from a time-invariant model is used for a_0 if it is not supplied (the same model you would get from `static_glm`). A diagonal matrix with large entries is recommended for Q_0 . What is large depends on the data set and model. Further, a covariance matrix for the first iteration Q is needed. The Q and a_0 are estimated with an EM-algorithm.

The model is specified through the `model` argument. The discrete outcome models are where outcomes are binned into the intervals. Be aware that there can be "loss" of information due to binning if outcomes are not discrete to start with. It is key for these models that the `id` argument is provided if individuals in the data set have time-varying covariates. The exponential model use a piecewise constant exponential distribution for the arrival times where there is no "loss" information due to binning. Though, one of the assumptions of the model is not satisfied if outcomes are only observed in discrete time intervals.

It is recommended to see the Shiny app demo for this function by calling `ddhazard_app()`.

Value

A list with class `ddhazard`. The list contains

<code>formula</code>	the passed formula.
<code>call</code>	the matched call.
<code>state_vecs</code>	2D matrix with the estimated state vectors (regression parameters) in each bin.
<code>state_vars</code>	3D array with smoothed variance estimates for each state vector.
<code>lag_one_cov</code>	3D array with lagged correlation matrix for each for each change in the state vector. Only present when the model is logit and the method is EKF.
<code>n_risk</code>	the number of observations in each interval.
<code>times</code>	the interval borders.
<code>risk_set</code>	the object from <code>get_risk_obj</code> if saved.
<code>data</code>	the data argument if saved.
<code>weights</code>	weights used in estimation if saved.
<code>id</code>	ids used to match rows in data to individuals.
<code>order</code>	order of the random walk.
<code>F_</code>	matrix which map from one state vector to the next.
<code>method</code>	method used in the E-step.
<code>est_Q_0</code>	TRUE if Q_0 was estimated in the EM-algorithm.
<code>family</code>	Rcpp Module with C++ functions used for estimation given the <code>model</code> argument.
<code>discrete_hazard_func</code>	the hazard function corresponding to the <code>model</code> argument.

terms the `terms` object used.
has_fixed_intercept TRUE if the model has a time-invariant intercept.
xlev a record of the levels of the factors used in fitting.

References

Fahrmeir, Ludwig. *Dynamic modelling and penalized likelihood estimation for discrete time survival data*. *Biometrika* 81.2 (1994): 317-330.

Durbin, James, and Siem Jan Koopman. *Time series analysis by state space methods*. No. 38. Oxford University Press, 2012.

Christoffersen, Benjamin. *dynamichazard: Dynamic Hazard Models Using State Space Models*. *Journal of Statistical Software* 99.7 (2021): 1-38.

See Also

[plot](#), [residuals](#), [predict](#), [static_glm](#), [ddhazard_app](#), [ddhazard_boot](#)

Examples

```

# example with first order model
library(dynamichazard)
fit <- ddhazard(
  Surv(time, status == 2) ~ log(bili), pbc, id = pbc$id, max_T = 3600,
  Q_0 = diag(1, 2), Q = diag(1e-4, 2), by = 50,
  control = ddhazard_control(method = "GMA"))
plot(fit)

# example with second order model
fit <- ddhazard(
  Surv(time, status == 2) ~ log(bili), pbc, id = pbc$id, max_T = 3600,
  Q_0 = diag(1, 4), Q = diag(1e-4, 2), by = 50,
  control = ddhazard_control(method = "GMA"),
  order = 2)
plot(fit)
  
```

ddhazard_app

ddhazard Demo

Description

ddhazard_app runs a shiny app with demonstration of models.

Usage

```
ddhazard_app(quietly = FALSE, ...)
```

Arguments

quietly TRUE if no messages should be printed when the app is run.
 ... starting values for the shiny app.

Details

Runs a shiny app where you try different model specifications on simulated data.

Value

Returns the object from shiny::shinyApp.

Examples

```
## Not run:
dynamichazard::ddhazard_app()
dynamichazard::ddhazard_app(seed = 1, more_options = TRUE)

## End(Not run)
```

ddhazard_boot	<i>Bootstrap for ddhazard Object</i>
---------------	--------------------------------------

Description

See the vignette vignette("Bootstrap_illustration", "dynamichazard"). The do_stratify_with_event may be useful when either cases or non-cases are very rare to ensure that the model estimation succeeds.

Usage

```
ddhazard_boot(
  ddhazard_fit,
  strata,
  unique_id,
  R = 100,
  do_stratify_with_event = FALSE,
  do_sample_weights = FALSE,
  LRs = ddhazard_fit$control$LR * 2^(0:(-4)),
  print_errors = FALSE
)
```

Arguments

ddhazard_fit	returned object from a ddhazard call.
strata	strata to sample within. These need to be on an individual by individual basis and not rows in the design matrix.
unique_id	unique ids where entries match entries of strata.
R	number of bootstrap estimates.
do_stratify_with_event	TRUE if sampling should be by strata of whether the individual has an event. An interaction factor will be made if strata is provided.
do_sample_weights	TRUE if weights should be sampled instead of individuals.
LRs	learning rates in decreasing order which will be used to estimate the model.
print_errors	TRUE if errors should be printed when estimations fails.

Value

An object like from the [boot](#) function.

See Also

[ddhazard](#), [plot](#)

Examples

```
library(dynamichazard)
set.seed(56219373)
fit <- ddhazard(
  Surv(time, status == 2) ~ log(bili), pbc, id = pbc$id, max_T = 3000,
  Q_0 = diag(1, 2), Q = diag(1e-4, 2), by = 100,
  control = ddhazard_control(method = "GMA"))
bt <- ddhazard_boot(fit, R = 999)
plot(fit, ddhazard_boot = bt, level = .9)
```

ddhazard_control

Auxiliary for Controlling Dynamic Hazard Models

Description

Auxiliary for additional settings with [ddhazard](#).

Usage

```

ddhazard_control(
  kappa = NULL,
  alpha = 1,
  beta = 0,
  NR_eps = NULL,
  LR = 1,
  n_max = 10^2,
  eps = 0.001,
  est_Q_0 = FALSE,
  method = "EKF",
  save_risk_set = TRUE,
  save_data = TRUE,
  eps_fixed_parems = 1e-04,
  fixed_parems_start = NULL,
  n_threads = getOption("ddhazard_max_threads"),
  denom_term = 1e-05,
  fixed_terms_method = "E_step",
  Q_0_term_for_fixed_E_step = NULL,
  permu = if (!is.null(method)) method == "SMA" else FALSE,
  posterior_version = "cholesky",
  GMA_max_rep = 25,
  GMA_NR_eps = 1e-04,
  est_a_0 = TRUE,
  ...
)

```

Arguments

kappa	hyper parameter κ in the unscented Kalman Filter.
alpha	hyper parameter α in the unscented Kalman Filter.
beta	hyper parameter β in the unscented Kalman Filter.
NR_eps	tolerance for the Extended Kalman filter. Default is NULL which means that no extra iteration is made in the correction step.
LR	learning rate.
n_max	maximum number of iteration in the EM-algorithm.
eps	tolerance parameter for the EM-algorithm
est_Q_0	TRUE if you want the EM-algorithm to estimate Q_0 . Default is FALSE.
method	set to the method to use in the E-step. Either "EKF" for the Extended Kalman Filter, "UKF" for the Unscented Kalman Filter, "SMA" for the sequential posterior mode approximation method or "GMA" for the global mode approximation method. "EKF" is the default.
save_risk_set	TRUE if you want to save the list from get_risk_obj used to estimate the model. It may be needed for later calls to e.g., residuals, plot and logLike.
save_data	TRUE if you want to keep the data argument. It may be needed for later calls to e.g., residuals, plot and logLike.

eps_fixed_parems	tolerance used in the M-step of the Fisher's scoring algorithm for the fixed effects
fixed_parems_start	starting value for fixed terms.
n_threads	maximum number of threads to use.
denom_term	term added to denominators in either the EKF or UKF.
fixed_terms_method	the method used to estimate the fixed effects. Either 'M_step' or 'E_step' for estimation in the M-step or E-step respectively.
Q_0_term_for_fixed_E_step	the diagonal value of the initial covariance matrix, Q_0 , for the fixed effects if fixed effects are estimated in the E-step.
permu	TRUE if the risk sets should be permuted before computation. This is TRUE by default for posterior mode approximation method and FALSE for all other methods.
posterior_version	the implementation version of the posterior approximation method. Either "woodbury" or "cholesky".
GMA_max_rep	maximum number of iterations in the correction step if method = 'GMA'.
GMA_NR_eps	tolerance for the convergence criteria for the relative change in the norm of the coefficients in the correction step if method = 'GMA'.
est_a_0	FALSE if the starting value of the state model should be fixed.
...	additional undocumented arguments.

Value

A list with components named as the arguments.

See Also

[ddhazard](#)

get_cloud_means	<i>Compute Mean Estimates from Particle Cloud</i>
-----------------	---

Description

Computes the estimated means from a particle cloud.

Usage

```

get_cloud_means(object, ...)

## S3 method for class 'PF_EM'
get_cloud_means(object, ...)

## S3 method for class 'PF_clouds'
get_cloud_means(
  object,
  cov_index = NULL,
  type = c("smoothed_clouds", "forward_clouds", "backward_clouds"),
  ...
)

```

Arguments

object	object with class PF_EM or PF_clouds.
...	named arguments to pass to the PF_clouds method.
cov_index	integer vector with indices of the random effect to include.
type	character with the type of cloud to compute means for.

Value

A matrix which rows are time indices and columns are random effect indices.

get_cloud_quantiles *Compute Quantile Estimates from Particle Cloud*

Description

Computes the estimated quantiles from a particle cloud.

Usage

```

get_cloud_quantiles(object, ...)

## S3 method for class 'PF_EM'
get_cloud_quantiles(object, ...)

## S3 method for class 'PF_clouds'
get_cloud_quantiles(
  object,
  cov_index = NULL,
  qlvls = c(0.05, 0.5, 0.95),
  type = c("smoothed_clouds", "forward_clouds", "backward_clouds"),
  ...
)

```

Arguments

object	object with class PF_EM or PF_clouds.
...	named arguments to pass to the PF_clouds method.
cov_index	integer vector with indices of the random effect to include.
qlvls	numeric vector with values in $[0, 1]$ with the quantiles to compute.
type	character with the type of cloud to compute quantiles for.

Value

A 3 dimensional array where the first dimension is the quantiles, the second dimension is the random effect, and the third dimension is the time.

get_Q_0	<i>Compute Time-Invariant Covariance Matrix</i>
---------	---

Description

Computes the invariant covariance matrix for a vector autoregression model.

Usage

```
get_Q_0(Qmat, Fmat)
```

Arguments

Qmat	covariance matrix in transition density.
Fmat	coefficients in transition density.

Value

The invariant covariance matrix.

Examples

```
Fmat <- matrix(c(.8, .4, .1, .5), 2, 2)
Qmat <- matrix(c(1, .5, .5, 2), 2)

x1 <- get_Q_0(Qmat = Qmat, Fmat = Fmat)
x2 <- Qmat
for(i in 1:101)
  x2 <- tcrossprod(Fmat %**% x2, Fmat) + Qmat
stopifnot(isTRUE(all.equal(x1, x2)))
```

get_risk_obj	<i>Risk Set on an Equidistant Distant Grid</i>
--------------	--

Description

Get the risk set at each bin over an equidistant distant grid.

Usage

```
get_risk_obj(
  Y,
  by,
  max_T,
  id,
  is_for_discrete_model = TRUE,
  n_threads = 1,
  min_chunk = 5000
)
```

Arguments

Y	vector of outcome variable returned from Surv .
by	length of each bin.
max_T	last observed time.
id	vector with ids where entries match with outcomes Y.
is_for_discrete_model	TRUE if the model outcome is discrete. For example, a logit model is discrete whereas what is referred to as the exponential model in this package is a dynamic model.
n_threads	set to a value greater than one to use mclapply to find the risk object.
min_chunk	minimum chunk size of ids to use when parallel version is used.

Value

a list with the following elements

risk_sets	list of lists with one for each bin. Each of the sub lists have indices that corresponds to the entries of Y that are at risk in the bin.
min_start	start time of the first bin.
I_len	length of each bin.
d	number of bins.
is_event_in	indices for which bin an observation Y is an event. -1 if the individual does not die in any of the bins.
is_for_discrete_model	value of is_for_discrete_model argument.

Examples

```
# small toy example with time-varying covariates
dat <- data.frame(
  id      = c(1, 1, 2, 2),
  tstart  = c(0, 4, 0, 2),
  tstop   = c(4, 6, 2, 4),
  event   = c(0, 1, 0, 0))

with(dat, get_risk_obj(Surv(tstart, tstop, event), by = 1, max_T = 6, id = id))
```

```
get_survival_case_weights_and_data
```

Get data.frame for Discrete Time Survival Models

Description

Function used to get data.frame with weights for a static fit for survivals.

Usage

```
get_survival_case_weights_and_data(
  formula,
  data,
  by,
  max_T,
  id,
  init_weights,
  risk_obj,
  use_weights = TRUE,
  is_for_discrete_model = TRUE,
  c_outcome = "Y",
  c_weights = "weights",
  c_end_t = "t"
)
```

Arguments

formula	coxph like formula with <code>Surv(tstart, tstop, event)</code> on the left hand site of <code>~</code> .
data	data.frame or environment containing the outcome and covariates.
by	interval length of the bins in which parameters are fixed.
max_T	end of the last interval interval.
id	vector of ids for each row of the in the design matrix.
init_weights	weights for the rows in data. Useful e.g., with skewed sampling.

risk_obj a pre-computed result from a [get_risk_obj](#). Will be used to skip some computations.
use_weights TRUE if weights should be used. See details.
is_for_discrete_model TRUE if the model is for a discrete hazard model is used like the logistic model.
c_outcome, c_weights, c_end_t alternative names to use for the added columns described in the return section. Useful if you already have a column named Y, t or weights.

Details

This function is used to get the `data.frame` for e.g. a `glm` fit that is comparable to a [ddhazard](#) fit in the sense that it is a static version. For example, say that we bin our time periods into $(0, 1]$, $(1, 2]$ and $(2, 3]$. Next, consider an individual who dies at time 2.5. He should be a control in the the first two bins and should be a case in the last bin. Thus the rows in the final data frame for this individual is `c(Y = 1, ..., weights = 1)` and `c(Y = 0, ..., weights = 2)` where Y is the outcome, ... is the covariates and weights is the weights for the regression. Consider another individual who does not die and we observe him for all three periods. Thus, he will yield one row with `c(Y = 0, ..., weights = 3)`.

This function use similar logic as the `ddhazard` for individuals with time varying covariates (see the vignette `vignette("ddhazard", "dynamichazard")` for details).

If `use_weights = FALSE` then the two previously mentioned individuals will yield three rows each. The first individual will have `c(Y = 0, t = 1, ..., weights = 1)`, `c(Y = 0, t = 2, ..., weights = 1)`, `c(Y = 1, t = 3, ..., weights = 1)` while the latter will have three rows `c(Y = 0, t = 1, ..., weights = 1)`, `c(Y = 0, t = 2, ..., weights = 1)`, `c(Y = 0, t = 3, ..., weights = 1)`. This kind of data frame is useful if you want to make a fit with e.g. `gam` function in the `mgcv` package as described en Tutz et. al (2016).

Value

Returns a `data.frame` where the following is added (column names will differ if you specified them): column Y for the binary outcome, column weights for weights of each row and additional rows if applicable. A column t is added for the stop time of the bin if `use_weights = FALSE`. An element Y with the used Surv object is added if `is_for_discrete_model = FALSE`.

References

Tutz, Gerhard, and Matthias Schmid. *Nonparametric Modeling and Smooth Effects*. Modeling Discrete Time-to-Event Data. Springer International Publishing, 2016. 105-127.

See Also

[ddhazard](#), [static_glm](#)

Examples

```
library(dynamichazard)
# small toy example with time-varying covariates
```

```

dat <- data.frame(
  id    = c( 1, 1, 2, 2),
  tstart = c( 0, 4, 0, 2),
  tstop  = c( 4, 6, 2, 6),
  event  = c( 0, 1, 0, 0),
  x1     = c(1.09, 1.29, 0, -1.16))

get_survival_case_weights_and_data(
  Surv(tstart, tstop, event) ~ x1, dat, by = 1, id = dat$id)$X
get_survival_case_weights_and_data(
  Surv(tstart, tstop, event) ~ x1, dat, by = 1, id = dat$id,
  use_weights = FALSE)$X

```

hatvalues.ddhazard *Hat Values for ddhazard Object*

Description

Computes hat-"like" values from usual L2 penalized binary regression.

Usage

```

## S3 method for class 'ddhazard'
hatvalues(model, ...)

```

Arguments

model	a fit from ddhazard .
...	not used.

Details

Computes hat-"like" values in each interval for each individual at risk in the interval. See the vignette("ddhazard", "dynamichazard") vignette for details.

Value

A list of matrices. Each matrix has three columns: the hat values, the row number of the original data point and the id the row belongs to.

See Also

[ddhazard](#)

Examples

```
library(dynamichazard)
fit <- ddhazard(
  Surv(time, status == 2) ~ log(bili), pbc, id = pbc$id, max_T = 3000,
  Q_0 = diag(1, 2), Q = diag(1e-4, 2), by = 100,
  control = ddhazard_control(method = "GMA"))
hvs <- hatvalues(fit)
head(hvs[[1]])
head(hvs[[2]])
```

 hds

Hard Drive Failures

Description

A data set containing hard drive failures data from Backblaze in the start-stop format used in the survival package.

Usage

hds

Format

A data frame with the following columns:

serial_number Serial number for the hard disk which the row belongs to.

model hard disk model.

manufacturer manufacturer of the hard disk model.

tstart,tstop start and stop times on the SMART 9 attribute scale.

fails 1 if the hard disk fails at tstop.

size_tb hard disk size in terabytes.

smart_x the raw SMART attribute x value. E.g., smart_12 is the power cycle count.

smart_x_bin 1 if the SMART attribute x value is non-zero.

..._cumsum cumulative sum of the prefix

n_fails number of failures in the original data. Hard disk should only fail once but this is not the case in the raw data.

n_records number of records in the original source.

min_date,max_date first and last date in the original source.

min_hours,max_hours smallest and largest value of the SMART 9 attribute in the original source.

Details

Details about the the SMART attributes can be found on <https://en.wikipedia.org/wiki/S.M.A.R.T.> As stated in the original source

"Reported stats for the same SMART stat can vary in meaning based on the drive manufacturer and the drive model. Make sure you are comparing apples-to-apples as drive manufacturers don't generally disclose what their specific numbers mean."

There are some notes on <https://en.wikipedia.org/wiki/S.M.A.R.T.> regarding which attributes that have vendor specific raw value. Further,

"The values in the files are the values reported by the drives. Sometimes, those values are out of whack. For example, in a few cases the RAW value of SMART 9 (Drive life in hours) reported a value that would make a drive 10+ years old, which was not possible. In other words, it's a good idea to have bounds checks when you process the data."

See this github page for the processing steps https://github.com/boennecd/backblaze_survival_analysis_prep.

Source

Raw data from <https://www.backblaze.com/b2/hard-drive-test-data.html>. Data have been processed to get a start-stop data.frame format.

 logLik.ddhazard

Log Likelihood of Mean Path of ddhazard Object

Description

Computes the log likelihood of (a potentially new) data set given the estimated:

$$E_{\theta}(\alpha_1|y_{1:d}), E_{\theta}(\alpha_2|y_{1:d}), \dots, E_{\theta}(\alpha_d|y_{1:d})$$

of the ddhazard object. Note that this is not the log likelihood of the observed data given the outcome.

Usage

```
## S3 method for class 'ddhazard'
logLik(object, data = NULL, id, ...)
```

Arguments

object	an object of class ddhazard.
data	new data to evaluate the likelihood for.
id	the individual identifiers as in ddhazard .
...	unused.

Value

Returns an object of class logLik. See [logLik](#).

Examples

```
library(dynamichazard)
fit <- ddhazard(
  Surv(time, status == 2) ~ log(bili), pbc, id = pbc$id, max_T = 3600,
  Q_0 = diag(1, 2), Q = diag(1e-4, 2), by = 50,
  control = ddhazard_control(method = "GMA"))
logLik(fit)
```

logLik.PF_EM

Approximate Log-Likelihood from a Particle Filter

Description

Computes the approximate log-likelihood using the forward filter clouds. See the vignette("Particle_filtering", "dynamichazard") for details.

Usage

```
## S3 method for class 'PF_EM'
logLik(object, ...)

## S3 method for class 'PF_clouds'
logLik(object, df = NA_real_, nobs = NA_integer_, ...)
```

Arguments

object	an object of class PF_clouds or PF_EM.
...	unused.
df	degrees of freedom used in the model.
nobs	integer with number of individuals used to estimate the model.

Value

The approximate log-likelihood value given the observed data and set of parameter used when simulating the clouds. An attribute "P(y_t|y_{1:(t-1)})" has the $P(y_t|y_{1:(t-1)})$ terms.

PF_control

*Auxiliary for Controlling Particle Fitting***Description**

Auxiliary for additional settings with [PF_EM](#).

Usage

```
PF_control(
  N_fw_n_bw = NULL,
  N_smooth = NULL,
  N_first = NULL,
  eps = 0.01,
  forward_backward_ESS_threshold = NULL,
  method = "AUX_normal_approx_w_cloud_mean",
  n_max = 25,
  n_threads = getOption("ddhazard_max_threads"),
  smoother = "Fearnhead_0_N",
  Q_tilde = NULL,
  est_a_0 = TRUE,
  N_smooth_final = N_smooth,
  nu = 0L,
  covar_fac = -1,
  ftol_rel = 1e-08,
  averaging_start = -1L,
  fix_seed = TRUE
)
```

Arguments

N_fw_n_bw	number of particles to use in forward and backward filter.
N_smooth	number of particles to use in particle smoother.
N_first	number of particles to use at time 0 and time $d + 1$.
eps	convergence threshold in EM method.
forward_backward_ESS_threshold	required effective sample size to not re-sample in the particle filters.
method	method for forward, backward and smoothing filter.
n_max	maximum number of iterations of the EM algorithm.
n_threads	maximum number threads to use in the computations.
smoother	smoother to use.
Q_tilde	covariance matrix of additional error term to add to the proposal distributions. NULL implies no additional error term.

est_a_0	FALSE if the starting value of the state model should be fixed. Does not apply for type = "VAR".
N_smooth_final	number of particles to sample with replacement from the smoothed particle cloud with N_smooth particles using the particles' weights. This causes additional sampling error but decreases the computation time in the M-step.
nu	integer with degrees of freedom to use in the (multivariate) t-distribution used as the proposal distribution. A (multivariate) normal distribution is used if it is zero.
covar_fac	factor to scale the covariance matrix with. Ignored if the values is less than or equal to zero.
ftol_rel	relative convergence tolerance of the mode objective in mode approximation.
averaging_start	index to start averaging. Values less then or equal to zero yields no averaging.
fix_seed	TRUE if the same seed should be used. E.g., in PF_EM the same seed will be used in each iteration of the E-step of the MCEM algorithm.

Details

The method argument can take the following values

- bootstrap_filter for a bootstrap filter.
- PF_normal_approx_w_cloud_mean for a particle filter where a Gaussian approximation is used using a Taylor approximation made at the mean for the current particle given the mean of the parent particles and/or mean of the child particles.
- AUX_normal_approx_w_cloud_mean for an auxiliary particle filter version of PF_normal_approx_w_cloud_mean.
- PF_normal_approx_w_particles for a filter similar to PF_normal_approx_w_cloud_mean and differs by making a Taylor approximation at a mean given each sampled parent and/or child particle.
- AUX_normal_approx_w_particles for an auxiliary particle filter version of PF_normal_approx_w_particles.

The smoother argument can take the following values

- Fearnhead_0_N for the smoother in Fearnhead, Wyncoll, and Tawn (2010).
- Brier_0_N_square for the smoother in Briers, Doucet, and Maskell (2010).

Value

A list with components named as the arguments.

References

- Gordon, N. J., Salmond, D. J., and Smith, A. F. (1993) Novel approach to nonlinear/non-Gaussian Bayesian state estimation. In *IEE Proceedings F (Radar and Signal Processing)*, (Vol. 140, No. 2, pp. 107-113). IET Digital Library.
- Pitt, M. K., and Shephard, N. (1999) Filtering via simulation: Auxiliary particle filters. *Journal of the American statistical association*, **94(446)**, 590-599.

Fearnhead, P., Wyncoll, D., and Tawn, J. (2010) A sequential smoothing algorithm with linear computational cost. *Biometrika*, **97**(2), 447-464.

Briers, M., Doucet, A., and Maskell, S. (2010) Smoothing algorithms for state-space models. *Annals of the Institute of Statistical Mathematics*, **62**(1), 61.

See Also

[PF_EM](#)

PF_EM

EM Estimation with Particle Filters and Smoothers

Description

Method to estimate the hyper parameters with an EM algorithm.

Usage

```
PF_EM(  
  formula,  
  data,  
  model = "logit",  
  by,  
  max_T,  
  id,  
  a_0,  
  Q_0,  
  Q,  
  order = 1,  
  control = PF_control(...),  
  trace = 0,  
  seed = NULL,  
  type = "RW",  
  fixed = NULL,  
  random = NULL,  
  Fmat,  
  fixed_effects,  
  G,  
  theta,  
  J,  
  K,  
  psi,  
  phi,  
  ...  
)
```

Arguments

formula	coxph like formula with <code>Surv(tstart, tstop, event)</code> on the left hand side of <code>~</code> .
data	data.frame or environment containing the outcome and covariates.
model	either 'logit' for binary outcomes with the logistic link function, 'cloglog' for binary outcomes with the inverse cloglog link function, or 'exponential' for piecewise constant exponential distributed arrival times.
by	interval length of the bins in which parameters are fixed.
max_T	end of the last interval interval.
id	vector of ids for each row of the in the design matrix.
a_0	vector a_0 for the initial coefficient vector for the first iteration (optional). Default is estimates from static model (see <code>static_glm</code>).
Q_0	covariance matrix for the prior distribution.
Q	initial covariance matrix for the state equation.
order	order of the random walk.
control	see <code>PF_control</code> .
trace	argument to get progress information. Zero will yield no info and larger integer values will yield incrementally more information.
seed	seed to set at the start of every EM iteration. See <code>set.seed</code> .
type	type of state model. Either "RW" for a [R]andom [W]alk or "VAR" for [V]ector [A]uto[R]egression.
fixed	two-sided <code>formula</code> to be used with random instead of formula. It is of the form <code>Surv(tstart, tstop, event) ~ x</code> or <code>Surv(tstart, tstop, event) ~ -1</code> for no fixed effects.
random	one-sided <code>formula</code> to be used with fixed instead of formula. It is of the form <code>~ z</code> .
Fmat	starting value for F when type = "VAR". See 'Details' in <code>PF_EM</code> .
fixed_effects	starting values for fixed effects if any. See <code>ddFixed</code> .
G, theta, J, K, psi, phi	parameters for a restricted type = "VAR" model. See the vignette mentioned in 'Details' of <code>PF_EM</code> and the examples linked to in 'See Also'.
...	optional way to pass arguments to control.

Details

Estimates a state model of the form

$$\alpha_t = F\alpha_t + R\epsilon_t, \quad \epsilon_t \sim N(0, Q)$$

where $F \in \mathbb{R}^{p \times p}$ has full rank, $\alpha_t \in \mathbb{R}^p$, $\epsilon_t \in \mathbb{R}^r$, $r \leq p$, and $R = (e_{l_1}, e_{l_2}, \dots, e_{l_r})$ where e_k is column from the p dimensional identity matrix and $l_1 < l_2 < \dots < l_r$. The time zero state is drawn from

$$\alpha_0 \sim N(a_0, Q_0)$$

with $Q_0 \in \mathbb{R}^{p \times p}$. The latent states, α_t , are related to the output through the linear predictors

$$\eta_{it} = X_t(R^+ \alpha_t) + Z_t \beta$$

where $X_t \in \mathbb{R}^{n_t \times r}$ and $Z_t \in \mathbb{R}^{n_t \times c}$ are design matrices and the outcome for a individual i at time t is distributed according to an exponential family member given η_{it} . β are constant coefficients.

See vignette("Particle_filtering", "dynamichazard") for details.

Value

An object of class PF_EM.

Warning

The function is still under development so the output and API may change.

See Also

[PF_forward_filter](#) to get a more precise estimate of the final log-likelihood.

See the examples at <https://github.com/boennecd/dynamichazard/tree/master/examples>.

Examples

```
#####
# Fit model with lung data set from survival
# Warning: long-ish computation time

library(dynamichazard)
.lung <- lung[!is.na(lung$ph.ecog), ]
# standardize
.lung$age <- scale(.lung$age)

# fit
set.seed(43588155)
pf_fit <- PF_EM(
  Surv(time, status == 2) ~ ddFixed(ph.ecog) + age,
  data = .lung, by = 50, id = 1:nrow(.lung),
  Q_0 = diag(1, 2), Q = diag(.5^2, 2),
  max_T = 800,
  control = PF_control(
    # these number should be larger! Small for CRAN checks
    N_fw_n_bw = 100L, N_first = 250L, N_smooth = 100L,
    n_max = 50, eps = .001, Q_tilde = diag(.2^2, 2), est_a_0 = FALSE,
    n_threads = 2))
```

```

# Plot state vector estimates
plot(pf_fit, cov_index = 1)
plot(pf_fit, cov_index = 2)

# Plot log-likelihood
plot(pf_fit$log_likes)

#####
# example with fixed intercept

# prepare data
temp <- subset(pbc, id <= 312, select=c(id, sex, time, status, edema, age))
pbc2 <- tmerge(temp, temp, id=id, death = event(time, status))
pbc2 <- tmerge(pbc2, pbcseq, id=id, albumin = tdc(day, albumin),
              protime = tdc(day, protime), bili = tdc(day, bili))
pbc2 <- pbc2[, c("id", "tstart", "tstop", "death", "sex", "edema",
               "age", "albumin", "protime", "bili")]
pbc2 <- within(pbc2, {
  log_albumin <- log(albumin)
  log_protime <- log(protime)
  log_bili <- log(bili)
})

# standardize
for(c in c("age", "log_albumin", "log_protime", "log_bili"))
  pbc2[[c]] <- drop(scale(pbc2[[c]]))

# fit model with extended Kalman filter
ddf_fit <- ddhazard(
  Surv(tstart, tstop, death == 2) ~ ddFixed_intercept() + ddFixed(age) +
    ddFixed(edema) + ddFixed(log_albumin) + ddFixed(log_protime) + log_bili,
  pbc2, Q_0 = 100, Q = 1e-2, by = 100, id = pbc2$id,
  model = "exponential", max_T = 3600,
  control = ddhazard_control(eps = 1e-5, NR_eps = 1e-4, n_max = 1e4))
summary(ddf_fit)

# fit model with particle filter
set.seed(88235076)
pf_fit <- PF_EM(
  Surv(tstart, tstop, death == 2) ~ ddFixed_intercept() + ddFixed(age) +
    ddFixed(edema) + ddFixed(log_albumin) + ddFixed(log_protime) + log_bili,
  pbc2, Q_0 = 2^2, Q = ddf_fit$Q * 100, # use estimate from before
  by = 100, id = pbc2$id,
  model = "exponential", max_T = 3600,
  control = PF_control(
    # these number should be larger! Small for CRAN checks
    N_fw_n_bw = 100, N_smooth = 250, N_first = 100, eps = 1e-3,
    method = "AUX_normal_approx_w_cloud_mean", est_a_0 = FALSE,
    Q_tilde = as.matrix(.1^2),
    n_max = 25, # just take a few iterations as an example
    n_threads = 2))

```

```

# compare results
plot(ddfit)
plot(pf_fit)
sqrt(ddfit$Q * 100)
sqrt(pf_fit$Q)
rbind(ddfit$fixed_effects, pf_fit$fixed_effects)

#####
# simulation example with `random` and `fixed` argument and a restricted
# model

# g groups with k individuals in each
g <- 3L
k <- 400L

# matrices for state equation
p <- g + 1L
G <- matrix(0., p^2, 2L)
for(i in 1:p)
  G[i + (i - 1L) * p, 1L + (i == p)] <- 1L

theta <- c(.9, .8)
# coefficients in transition density
(F <- matrix(as.vector(G %%% theta), 4L, 4L))

J <- matrix(0., ncol = 2L, nrow = p)
J[-p, 1L] <- J[p, 2L] <- 1
psi <- c(log(c(.3, .1)))

K <- matrix(0., p * (p - 1L) / 2L, 2L)
j <- 0L
for(i in (p - 1L):1L){
  j <- j + i
  K[j, 2L] <- 1
}
K[K[, 2L] < 1, 1L] <- 1
phi <- log(-(c(.8, .3) + 1) / (c(.8, .3) - 1))

V <- diag(exp(drop(J %%% psi)))
C <- diag(1, ncol(V))
C[lower.tri(C)] <- 2/(1 + exp(-drop(K %%% phi))) - 1
C[upper.tri(C)] <- t(C)[upper.tri(C)]
(Q <- V %%% C %%% V) # covariance matrix in transition density
cov2cor(Q)

Q_0 <- get_Q_0(Q, F.) # time-invariant covariance matrix
beta <- c(rep(-6, g), 0) # all groups have the same long run mean intercept

# simulate state variables
set.seed(56219373)
n_periods <- 300L
alphas <- matrix(nrow = n_periods + 1L, ncol = p)

```

```

alphas[1L, ] <- rnorm(p) %%% chol(Q_0)
for(i in 1:n_periods + 1L)
  alphas[i, ] <- F. %%% alphas[i - 1L, ] + drop(rnorm(p) %%% chol(Q))

alphas <- t(t(alphas) + beta)

# plot state variables
matplot(alphas, type = "l", lty = 1)

# simulate individuals' outcome
n_obs <- g * k
df <- lapply(1:n_obs, function(i){
  # find the group
  grp <- (i - 1L) %/% (n_obs / g) + 1L

  # left-censoring
  tstart <- max(0L, sample.int((n_periods - 1L) * 2L, 1) - n_periods + 1L)

  # covariates
  x <- c(1, rnorm(1))

  # outcome (stop time and event indicator)
  osa <- NULL
  oso <- NULL
  osx <- NULL
  y <- FALSE
  for(tstop in (tstart + 1L):n_periods){
    sigmoid <- 1 / (1 + exp(- drop(x %%% alphas[tstop + 1L, c(grp, p)])))
    if(sigmoid > runif(1)){
      y <- TRUE
      break
    }
  }
  if(.01 > runif(1L) && tstop < n_periods){
    # sample new covariate
    osa <- c(osa, tstart)
    tstart <- tstop
    oso <- c(oso, tstop)
    osx <- c(osx, x[2])
    x[2] <- rnorm(1)
  }
})

cbind(
  tstart = c(osa, tstart), tstop = c(oso, tstop),
  x = c(osx, x[2]), y = c(rep(FALSE, length(osa)), y), grp = grp,
  id = i)
})
df <- data.frame(do.call(rbind, df))
df$grp <- factor(df$grp)

# fit model. Start with "cheap" iterations
fit <- PF_EM(
  fixed = Surv(tstart, tstop, y) ~ x, random = ~ grp + x - 1,

```

```

data = df, model = "logit", by = 1L, max_T = max(df$stop),
Q_0 = diag(1.5^2, p), id = df$id, type = "VAR",
G = G, theta = c(.5, .5), J = J, psi = log(c(.1, .1)),
K = K, phi = log(-(c(.4, 0) + 1) / (c(.4, 0) - 1)),
control = PF_control(
  N_fw_n_bw = 100L, N_smooth = 100L, N_first = 500L,
  method = "AUX_normal_approx_w_cloud_mean",
  nu = 5L, # sample from multivariate t-distribution
  n_max = 60L, averaging_start = 50L,
  smoother = "Fearnhead_0_N", eps = 1e-4, covar_fac = 1.2,
  n_threads = 2L # depends on your cpu(s)
),
trace = 1L)
plot(fit$log_likes) # log-likelihood approximation at each iterations

# you can take more iterations by uncommenting the following
# cl <- fit$call
# ctrl <- cl[["control"]]
# ctrl[c("N_fw_n_bw", "N_smooth", "N_first", "n_max",
#        "averaging_start")] <- list(500L, 2000L, 5000L, 200L, 30L)
# cl[["control"]] <- ctrl
# cl[c("phi", "psi", "theta")] <- list(fit$phi, fit$psi, fit$theta)
# fit_extra <- eval(cl)

plot(fit$log_likes) # log-likelihood approximation at each iteration

# check estimates
sqrt(diag(fit$Q))
sqrt(diag(Q))
cov2cor(fit$Q)
cov2cor(Q)
fit$F
F.

# plot predicted state variables
for(i in 1:p){
  plot(fit, cov_index = i)
  abline(h = 0, lty = 2)
  lines(1:nrow(alphas) - 1, alphas[, i] - beta[i], lty = 3)
}

```

Description

Functions to only use the forward particle filter. Useful for log-likelihood evaluation though there is an $O(d^2)$ variance of the estimate where d is the number of time periods. The number of particles specified in the control argument has no effect.

The function does not alter the `.Random.seed` to make sure the same `rng.kind` is kept after the call. See `PF_EM` for model details.

Usage

```
PF_forward_filter(x, N_fw, N_first, ...)  
  
## S3 method for class 'PF_EM'  
PF_forward_filter(x, N_fw, N_first, seed, ...)  
  
## S3 method for class 'formula'  
PF_forward_filter(  
  x,  
  N_fw,  
  N_first,  
  data,  
  model = "logit",  
  by,  
  max_T,  
  id,  
  a_0,  
  Q_0,  
  Q,  
  fixed_effects,  
  control = PF_control(...),  
  seed = NULL,  
  trace = 0,  
  G,  
  theta,  
  J,  
  K,  
  psi,  
  phi,  
  type = "RW",  
  Fmat,  
  ...  
)  
  
## S3 method for class 'data.frame'  
PF_forward_filter(  
  x,  
  N_fw,  
  N_first,  
  formula,  
  model = "logit",  
  by,  
  max_T,  
  id,  
  a_0,
```

```

    Q_0,
    Q,
    fixed_effects,
    control = PF_control(...),
    seed = NULL,
    trace = 0,
    fixed = NULL,
    random = NULL,
    G,
    theta,
    J,
    K,
    psi,
    phi,
    type = "RW",
    Fmat,
    order = 1,
    ...
)

```

Arguments

<code>x</code>	an PF_EM or formula object.
<code>N_fw</code>	number of particles.
<code>N_first</code>	number of time zero particles to draw.
<code>...</code>	optional way to pass arguments to control.
<code>seed</code>	<code>.GlobalEnv\$.Random.seed</code> to set. Not seed as in <code>set.seed</code> function. Can be used with the <code>.Random.seed</code> returned by <code>PF_EM</code> .
<code>data</code>	data.frame or environment containing the outcome and covariates.
<code>model</code>	either 'logit' for binary outcomes with the logistic link function, 'cloglog' for binary outcomes with the inverse cloglog link function, or 'exponential' for piecewise constant exponential distributed arrival times.
<code>by</code>	interval length of the bins in which parameters are fixed.
<code>max_T</code>	end of the last interval interval.
<code>id</code>	vector of ids for each row of the in the design matrix.
<code>a_0</code>	vector a_0 for the initial coefficient vector for the first iteration (optional). Default is estimates from static model (see <code>static_glm</code>).
<code>Q_0</code>	covariance matrix for the prior distribution.
<code>Q</code>	initial covariance matrix for the state equation.
<code>fixed_effects</code>	values for the fixed parameters.
<code>control</code>	see <code>PF_control</code> .
<code>trace</code>	argument to get progress information. Zero will yield no info and larger integer values will yield incrementally more information.

G, theta, J, K, psi, phi	parameters for a restricted type = "VAR" model. See the vignette mentioned in 'Details' of PF_EM and the examples linked to in 'See Also'.
type	type of state model. Either "RW" for a [R]andom [W]alk or "VAR" for [V]ector [A]uto[R]egression.
Fmat	starting value for F when type = "VAR". See 'Details' in PF_EM .
formula	coxph like formula with Surv (tstart, tstop, event) on the left hand side of \sim .
fixed	two-sided formula to be used with random instead of formula. It is of the form Surv (tstart, tstop, event) \sim x or Surv (tstart, tstop, event) \sim -1 for no fixed effects.
random	one-sided formula to be used with fixed instead of formula. It is of the form \sim z.
order	order of the random walk.

Value

An object of class PF_cclouds.

Methods (by class)

- `PF_EM`: Forward particle filter using the estimates of an [PF_EM](#) call.
- `formula`: Forward particle filter with formula input.
- `data.frame`: Forward particle filter with `data.frame` data input as `x` instead of `data`. Can be used with `fixed` and `random` argument.

Warning

The function is still under development so the output and API may change.

Examples

```
# head-and-neck cancer study data. See Efron, B. (1988) doi:10.2307/2288857
is_censored <- c(
  6, 27, 34, 36, 42, 46, 48:51, 51 + c(15, 30:28, 33, 35:37, 39, 40, 42:45))
head_neck_cancer <- data.frame(
  id = 1:96,
  stop = c(
    1, 2, 2, rep(3, 6), 4, 4, rep(5, 8),
    rep(6, 7), 7, 8, 8, 8, 9, 9, 10, 10, 10, 11, 14, 14, 14, 15, 18, 18, 20,
    20, 37, 37, 38, 41, 45, 47, 47,
    2, 2, 3, rep(4, 4), rep(5, 5), rep(6, 5),
    7, 7, 7, 9, 10, 11, 12, 15, 16, 18, 18, 18, 21,
    21, 24, 25, 27, 36, 41, 44, 52, 54, 59, 59, 63, 67, 71, 76),
  event = !(1:96 %in% is_censored),
  group = factor(c(rep(1, 45 + 6), rep(2, 45))))
```

```

# fit model
set.seed(61364778)
ctrl <- PF_control(
  N_fw_n_bw = 500, N_smooth = 2500, N_first = 2000,
  n_max = 1, # set to one as an example
  n_threads = 2,
  eps = .001, Q_tilde = as.matrix(.3^2), est_a_0 = FALSE)
pf_fit <- suppressWarnings(
  PF_EM(
    survival::Surv(stop, event) ~ ddFixed(group),
    data = head_neck_cancer, by = 1, Q_0 = 1, Q = 0.1^2, control = ctrl,
    max_T = 30))

# the log-likelihood in the final iteration
(end_log_like <- logLik(pf_fit))

# gives the same
fw_ps <- PF_forward_filter(
  survival::Surv(stop, event) ~ ddFixed(group), N_fw = 500, N_first = 2000,
  data = head_neck_cancer, by = 1, Q_0 = 1, Q = 0.1^2,
  a_0 = pf_fit$a_0, fixed_effects = -0.5370051,
  control = ctrl, max_T = 30, seed = pf_fit$seed)
all.equal(c(end_log_like), c(logLik(fw_ps)))

# will differ since we use different number of particles
fw_ps <- PF_forward_filter(
  survival::Surv(stop, event) ~ ddFixed(group), N_fw = 1000, N_first = 3000,
  data = head_neck_cancer, by = 1, Q_0 = 1, Q = 0.1^2,
  a_0 = pf_fit$a_0, fixed_effects = -0.5370051,
  control = ctrl, max_T = 30, seed = pf_fit$seed)
all.equal(c(end_log_like), c(logLik(fw_ps)))

# will differ since we use the final estimates
fw_ps <- PF_forward_filter(pf_fit, N_fw = 500, N_first = 2000)
all.equal(c(end_log_like), c(logLik(fw_ps)))

```

PF_get_score_n_hess *Approximate Observed Information Matrix and Score Vector*

Description

Returns a list of functions to approximate the observed information matrix and score vector.

Usage

```
PF_get_score_n_hess(object, debug = FALSE, use_O_n_sq = FALSE)
```

Arguments

object	object of class <code>PF_EM</code> .
debug	TRUE if debug information should be printed to the console.
use_0_n_sq	TRUE if the method from Poyiadjis et al. (2011) should be used.

Details

The score vector and observed information matrix are computed with the (forward) particle filter. This comes at an $O(d^2)$ variance where d is the number of periods. Thus, the approximation may be poor for long series. The score vector can be used to perform stochastic gradient descent.

If `use_0_n_sq` is TRUE then the method in Poyiadjis et al. (2011) is used. This may only have a variance which is linear in the number of time periods. However, the present implementation is $O(N^2)$ where N is the number of particles. The method uses a particle filter as in Section 3.1 of Lin et al. (2005). There is no need to call `run_particle_filter` unless one wants a new approximation of the log-likelihood as a separate filter is run with `get_get_score_n_hess` when `use_0_n_sq` is TRUE.

Value

A list with the following functions as elements

<code>run_particle_filter</code>	function to run particle filter as with <code>PF_forward_filter</code> .
<code>set_parameters</code>	function to set the parameters in the model. The first argument is a vectorized version of F matrix and Q matrix. The second argument is the fixed effect coefficients.
<code>set_n_particles</code>	sets the number of particles to use in <code>run_particle_filter</code> and <code>get_get_score_n_hess</code> when <code>use_0_n_sq</code> is TRUE.
<code>get_get_score_n_hess</code>	approximate the observed information matrix and score vector. The argument toggles whether or not to approximate the observed information matrix. The last particle cloud from <code>run_particle_filter</code> is used when <code>use_0_n_sq</code> is FALSE.

Warning

The function is still under development so the output and API may change.

References

- Cappe, O. and Moulines, E. (2005) Recursive Computation of the Score and Observed Information Matrix in Hidden Markov Models. *IEEE/SP 13th Workshop on Statistical Signal Processing*.
- Cappe, O., Moulines, E. and Ryden, T. (2005) Inference in Hidden Markov Models (Springer Series in Statistics). Springer-Verlag.
- Doucet, A., and Tadić, V. B. (2003) Parameter Estimation in General State-Space Models Using Particle Methods. *Annals of the Institute of Statistical Mathematics*, **55**(2), 409–422.

Lin, M. T., Zhang, J. L., Cheng, Q. and Chen, R. (2005) Independent Particle Filters. *Journal of the American Statistical Association*, **100(472)**, 1412-1421.

Poyiadjis, G., Doucet, A. and Singh, S. S. (2011) Particle Approximations of the Score and Observed Information Matrix in State Space Models with Application to Parameter Estimation. *Biometrika*, **98(1)**, 65–80.

See Also

See the examples at <https://github.com/boennecd/dynamichazard/tree/master/examples>.

Examples

```
library(dynamichazard)
.lung <- lung[!is.na(lung$ph.ecog), ]
# standardize
.lung$age <- scale(.lung$age)

# fit model
set.seed(43588155)
pf_fit <- PF_EM(
  fixed = Surv(time, status == 2) ~ ph.ecog + age,
  random = ~ 1, model = "exponential",
  data = .lung, by = 50, id = 1:nrow(.lung),
  Q_0 = as.matrix(1), Q = as.matrix(.5^2), type = "VAR",
  max_T = 800, Fmat = as.matrix(.5),
  control = PF_control(
    N_fw_n_bw = 250, N_first = 2000, N_smooth = 500, covar_fac = 1.1,
    nu = 6, n_max = 1000L, eps = 1e-4, averaging_start = 200L,
    n_threads = 2))

# compute score and observed information matrix
comp_obj <- PF_get_score_n_hess(pf_fit)
comp_obj$set_n_particles(N_fw = 10000L, N_first = 10000L)
comp_obj$run_particle_filter()
(o1 <- comp_obj$get_get_score_n_hess())

# O(N^2) method with lower variance as a function of time
comp_obj <- PF_get_score_n_hess(pf_fit, use_0_n_sq = TRUE)
comp_obj$set_n_particles(N_fw = 2500L, N_first = 2500L)
(o2 <- comp_obj$get_get_score_n_hess())

# approximations may have large variance
o3 <- replicate(10L, {
  runif(1)
  pf_fit$seed <- .Random.seed
  comp_obj <- PF_get_score_n_hess(pf_fit)
  comp_obj$set_n_particles(N_fw = 10000L, N_first = 10000L)
  comp_obj$run_particle_filter()
  comp_obj$get_get_score_n_hess()
}, simplify = FALSE)
sapply(o3, function(x) x$score)
```

```
sapply(o3, function(x) sqrt(diag(solve(x$obs_info))))
```

plot.ddhazard

Plots for ddhazard Object

Description

Plot of estimated state space variables from a [ddhazard](#) fit.

Usage

```
## S3 method for class 'ddhazard'
plot(
  x,
  xlab = "Time",
  ylab = "Hazard",
  type = "cov",
  plot_type = "l",
  cov_index,
  ylim,
  col = "black",
  add = FALSE,
  do_alter_mfcol = TRUE,
  level = 0.95,
  ddhazard_boot,
  ...
)
```

Arguments

x	result of ddhazard call.
xlab, ylab, ylim, col	arguments to override defaults set in the function.
type	type of plot. Currently, only "cov" is available for plot of the state space parameters.
plot_type	the type argument passed to plot.
cov_index	the index (indices) of the state space parameter(s) to plot.
add	FALSE if you want to make a new plot.
do_alter_mfcol	TRUE if the function should alter <code>par(mfcol)</code> in case that <code>cov_index</code> has more than one element.
level	level (fraction) for confidence bounds.
ddhazard_boot	object from a ddhazard_boot call which confidence bounds will be based on and where bootstrap samples will be printed with a transparent color.
...	arguments passed to plot.default or lines depending on the value of add.

Details

Creates a plot of state variables or adds state variables to a plot with indices `cov_index`. Pointwise 1.96 std. confidence intervals are provided with the smoothed co-variance matrices from the fit.

Value

Returns NULL using `invisible`.

Examples

```
library(dynamichazard)
fit <- ddhazard(
  Surv(time, status == 2) ~ log(bili), pbc, id = pbc$id, max_T = 3600,
  Q_0 = diag(1, 2), Q = diag(1e-4, 2), by = 50,
  control = ddhazard_control(method = "GMA"))
plot(fit)
plot(fit, cov_index = 2)
```

plot.ddhazard_space_errors

State Space Error Plot

Description

Plot function for state space errors from `ddhazard` fit.

Usage

```
## S3 method for class 'ddhazard_space_errors'
plot(
  x,
  mod,
  cov_index = NA,
  t_index = NA,
  p_cex = par()$cex * 0.2,
  pch = 16,
  ylab = "Std. state space error",
  x_tick_loc = NA,
  x_tick_mark = NA,
  xlab = "Time",
  ...
)
```

Arguments

x	result of <code>residuals</code> with a 'type' argument which yields state space errors.
mod	the <code>ddhazard</code> result used in the <code>residuals</code> call.
cov_index	the indices of state vector errors to plot. Default is to use all.
t_index	the bin indices to plot. Default is to use all bins.
p_cex	cex argument for the points
pch, ylab, xlab	arguments to override defaults set in the function.
x_tick_loc, x_tick_mark	at and labels arguments passed to axis.
...	arguments passed to <code>plot.default</code> .

Value

Returns NULL using `invisible`.

plot.ddsurvcurve	<i>Create and plot survival curves</i>
------------------	--

Description

The function creates a predicted survival curve for a new observation using a estimated `ddhazard` model from `ddhazard`. The predicted curve is based on the predicted mean path of the state vector. Thus, the survival curve will not be a "mean" curve due to the non-linear relation between the probability of an event and the state vector.

Usage

```
## S3 method for class 'ddsurvcurve'
plot(x, y, xlab = "Time", ylab = "Survival", ylim, xaxs = "i", yaxs = "i", ...)

## S3 method for class 'ddsurvcurve'
lines(x, col = "Black", lty = 1, lwd = par()$lwd, ...)

ddsurvcurve(object, new_data, tstart = "", tstop = "")
```

Arguments

x	a <code>ddsurvcurve</code> object.
y	not used.
xlab	xlab passed to plot.
ylab	ylab passed to plot.
ylim	ylim passed to plot.
xaxs	xaxs passed to plot.

yaxs	yaxs passed to plot.
...	not used.
col	col passed to lines.
lty	lty passed to lines.
lwd	lwd passed to lines.
object	a ddhazard object.
new_data	a data.frame with the new data for the observation who the survival curve should be for. It can have more rows if tstart and tstop is supplied. The rows need to be consecutive and non-overlapping time intervals.
tstart	name of the start time column in new_data. It must be on the same time scale as the tstart used in the <code>Surv(tstart, tstop, event)</code> in the formula passed to <code>ddhazard</code> .
tstop	same as tstart for the stop argument.

Value

ddsurvcurve returns an object of class ddsurvcurve. Its elements are the predicted discrete survival curve, time points for the survival curve, point of the first time period, the call, the discrete probabilities of an event in each interval conditional on survival up to that point, and the name of the distribution family. It should be seen as a plug-in estimate.

Methods (by generic)

- plot: method for plotting survival curve.
- lines: Method for adding survival curve to a plot.

plot.ddsurvcurve

Returns the same as `lines.ddsurvcurve`.

lines.ddsurvcurve

Either returns the objects used in the call to `segments` for discrete time hazard models, or the time points and survival function used to draw the survival curve.

See Also

[ddhazard](#), and [predict.ddhazard](#).

Examples

```
#####
# example with continuous time model
# setup data set. See `vignette("timedep", "survival")`
library(dynamichazard)
temp <- subset(pbc, id <= 312, select=c(id:sex, stage))
pbc2 <- tmerge(temp, temp, id=id, death = event(time, status))
pbc2 <- tmerge(pbc2, pbcseq, id = id, bili = tdc(day, bili))
```

```

# fit model
f1 <- ddhazard(
  Surv(tstart, tstop, death == 2) ~ ddFixed(log(bili)), pbc2, id = pbc2$id,
  max_T = 3600, Q_0 = 1, Q = 1e-2, by = 100, model = "exponential",
  control = ddhazard_control(method = "EKF", eps = 1e-4, n_max = 1000,
    fixed_terms_method = "M_step"))

# predict with default which is all covariates set to zero
ddcurve <- ddsurvcurve(f1)
par_old <- par(mar = c(4.5, 4, .5, .5))
plot(ddcurve, col = "DarkBlue", lwd = 2)

# compare with cox model
f2 <- coxph(Surv(tstart, tstop, death == 2) ~ log(bili), data = pbc2)
nw <- data.frame(bili = 1, tstart = 0, tstop = 3000)
lines(survfit(f2, newdata = nw))

# same as above but with bili = 3
nw <- data.frame(bili = 3)
lines(ddsurvcurve(f1, new_data = nw), col = "DarkBlue")
lines(survfit(f2, newdata = nw))

# change to time-varying slope
f3 <- ddhazard(
  Surv(tstart, tstop, death == 2) ~ log(bili), pbc2, id = pbc2$id,
  max_T = 3600, Q_0 = diag(1, 2), Q = diag(1e-2, 2), by = 100, model = "exponential",
  control = ddhazard_control(method = "EKF", eps = 1e-4, n_max = 1000))

# example with time-varying coefficient
nw <- data.frame(
  bili = c(2.1, 1.9, 3.3, 3.9, 3.8, 3.6, 4, 4.9, 4.2, 5.7, 10.2),
  tstart = c(0L, 225L, 407L, 750L, 1122L, 1479L, 1849L, 2193L, 2564L, 2913L,
    3284L),
  tstop = c(225L, 407L, 750L, 1122L, 1479L, 1849L, 2193L, 2564L, 2913L,
    3284L, 3600L))
ddcurve <- ddsurvcurve(f3, new_data = nw, tstart = "tstart", tstop = "tstop")
lines(ddcurve, "darkorange", lwd = 2)

# can condition on survival up to some time
ddcurve <- ddsurvcurve(f3, new_data = nw[-(1:5), ], tstart = "tstart",
  tstop = "tstop")
lines(ddcurve, lty = 2, lwd = 2)

#####
# example with discrete time model
# head-and-neck cancer study data. See Efron, B. (1988) doi:10.2307/2288857
is_censored <- c(
  6, 27, 34, 36, 42, 46, 48:51, 51 + c(15, 30:28, 33, 35:37, 39, 40, 42:45))
head_neck_cancer <- data.frame(
  id = 1:96,
  stop = c(
    1, 2, 2, rep(3, 6), 4, 4, rep(5, 8),

```

```

rep(6, 7), 7, 8, 8, 8, 9, 9, 10, 10, 10, 11, 14, 14, 14, 15, 18, 18, 20,
20, 37, 37, 38, 41, 45, 47, 47,
2, 2, 3, rep(4, 4), rep(5, 5), rep(6, 5),
7, 7, 7, 9, 10, 11, 12, 15, 16, 18, 18, 18, 21,
21, 24, 25, 27, 36, 41, 44, 52, 54, 59, 59, 63, 67, 71, 76),
event = !(1:96 %in% is_censored),
group = factor(c(rep(1, 45 + 6), rep(2, 45))))

# fit model
h1 <- ddhazard(
  Surv(stop, event) ~ group, head_neck_cancer, by = 1, max_T = 45,
  Q_0 = diag(2^2, 2), Q = diag(.01^2, 2), control = ddhazard_control(
    method = "GMA", eps = 1e-4, n_max = 200))

# plot predicted survival curve. Notice the steps since the model is discrete
nw <- data.frame(group = factor(1, levels = 1:2), tstart = 0, tstop = 30)
ddcurve <- ddsurvcurve(h1, new_data = nw, tstart = "tstart",
  tstop = "tstop")
plot(ddcurve, col = "Darkblue")

nw$group <- factor(2, levels = 1:2)
ddcurve <- ddsurvcurve(h1, new_data = nw, tstart = "tstart",
  tstop = "tstop")
lines(ddcurve, col = "DarkOrange")

# compare with KM
lines(survfit(Surv(stop, event) ~ 1, head_neck_cancer, subset = group == 1),
  col = "DarkBlue")
lines(survfit(Surv(stop, event) ~ 1, head_neck_cancer, subset = group == 2),
  col = "DarkOrange")
par(par_old) # As per CRAN policy, the settings are reset

```

plot.PF_clouds

Plot of Clouds from a PF_clouds Object

Description

Plots mean curve along with quantiles through time for the forward, backward or smoothed clouds.

Usage

```

## S3 method for class 'PF_clouds'
plot(
  x,
  y,
  type = c("smoothed_clouds", "forward_clouds", "backward_clouds"),
  ylim,
  add = FALSE,
  qlvls = c(0.05, 0.5, 0.95),

```

```

    pch = 4,
    lty = 1,
    col,
    ...,
    cov_index,
    qtype = c("points", "lines")
)

```

Arguments

x	an object of class PF_clouds.
y	unused.
type	parameter to specify which cloud to plot.
ylim	ylim passed to matplot .
add	TRUE if a new plot should not be made.
qlvls	vector of quantile levels to be plotted.
pch	pch argument for the quantile points.
lty	lty argument for the mean curves.
col	col argument to matplot and matpoints or matlines .
...	unused.
cov_index	indices of the state vector to plot. All are plotted if this argument is omitted.
qtype	character specifying how to show quantiles. Either "points" for crosses or "lines" for dashed lines.

Value

List with quantile levels and mean curve.

plot.PF_EM	<i>Plot for a PF_EM Object</i>
------------	--------------------------------

Description

Short hand to call [plot.PF_clouds](#).

Usage

```

## S3 method for class 'PF_EM'
plot(x, y, ...)

```

Arguments

x	an object of class PF_EM.
y	unused.
...	arguments to plot.PF_clouds .

Value

See [plot.PF_clouds](#)

predict.ddhazard	<i>Predict Method for ddhazard Object</i>
------------------	---

Description

Predict method for [ddhazard](#).

Usage

```
## S3 method for class 'ddhazard'
predict(
  object,
  new_data,
  type = c("response", "term"),
  tstart = "start",
  tstop = "stop",
  use_parallel,
  sds = FALSE,
  max_threads,
  ...
)
```

Arguments

object	result of a ddhazard call.
new_data	new data to base predictions on.
type	either "response" for predicted probability of an event or "term" for predicted terms in the linear predictor.
tstart	name of the start time column in new_data. It must be on the same time scale as the tstart used in the Surv(tstart, tstop, event) in the formula passed to ddhazard .
tstop	same as tstart for the stop argument.
use_parallel	not longer supported.
sds	TRUE if point wise standard deviation should be computed. Convenient if you use functions like ns and you only want one term per term in the right hand site of the formula used in ddhazard .
max_threads	not longer supported.
...	not used.

Details

The function check if there are columns in `new_data` which names match `tstart` and `tstop`. If matched, then the bins are found which the start time to the stop time are in. If `tstart` and `tstop` are not matched then all the bins used in the estimation method will be used.

Value

Returns a list with elements as described in the Term and Response sections.

Term

The result with `type = "term"` is a lists of list each having length equal to `nrow(new_data)`. The lists are

`terms` It's elements are matrices where the first dimension is time and the second dimension is the terms.

`sds` similar to `terms` for the point-wise confidence intervals using the smoothed co-variance matrices. Only added if `sds = TRUE`.

`fixed_terms` contains the fixed (non-time-varying) effect.

`varcov` similar to `sds` but differs by containing the whole covariance matrix for the terms. It is a 3D array where the third dimension is time. Only added if `sds = TRUE`.

`start` numeric vector with start time for each time-varying term.

`tstop` numeric vector with stop time for each time-varying term.

Response

The result with `type = "response"` is a list with the elements below. If `tstart` and `tstop` are matched in columns in `new_data`, then the probability will be for having an event between `tstart` and `tstop` conditional on no events before `tstart`.

`fits` fitted probability of an event.

`istart` numeric vector with start time for each element in `fits`.

`istop` numeric vector with stop time for each element in `fits`.

Examples

```
fit <- ddhazard(
  Surv(time, status == 2) ~ log(bili), pbc, id = pbc$id, max_T = 3600,
  Q_0 = diag(1, 2), Q = diag(1e-4, 2), by = 50,
  control = ddhazard_control(method = "GMA"))
predict(fit, type = "response", new_data =
  data.frame(time = 0, status = 2, bili = 3))
predict(fit, type = "term", new_data =
  data.frame(time = 0, status = 2, bili = 3))

# probability of an event between time 0 and 2000 with bili = 3
predict(fit, type = "response", new_data =
  data.frame(time = 0, status = 2, bili = 3, tstart = 0, tstop = 2000),
  tstart = "tstart", tstop = "tstop")
```

```
print.ddhazard_boot
```

Summary Statistics for a ddhazard_boot Object

Description

Arguments have the same effects as for an object from a [boot](#) call. See [print](#).

Usage

```
## S3 method for class 'ddhazard_boot'
print(x, digits = getOption("digits"), index = 1L:ncol(boot.out$t), ...)
```

Arguments

<code>x</code>	returned object from a ddhazard_boot call.
<code>digits</code>	the number of digits to be printed in the summary statistics.
<code>index</code>	indices indicating for which elements of the bootstrap output summary statistics are required.
<code>...</code>	not used.

Value

Returns `x` using [invisible](#).

See Also

[ddhazard_boot](#)

```
print.summary.ddhazard
```

Summarizing Dynamic Hazard Models Fits

Description

The `sd` printed for time-varying effects are point-wise standard deviations from the smoothed covariance matrices.

Usage

```
## S3 method for class 'summary.ddhazard'
print(x, digits = getOption("digits"), ...)

## S3 method for class 'ddhazard'
summary(object, var_indices = 1:ncol(object$state_vecs), max_print = 10, ...)
```

Arguments

x	object returned from <code>summary.ddhazard</code> .
digits	number of digits to print.
...	not used.
object	object returned from <code>ddhazard</code> .
var_indices	variable indices to print for time-varying effects.
max_print	maximum number of time points to print coefficients at.

residuals.ddhazard *Residuals Method for ddhazard Object*

Description

Residuals method for the result of a `ddhazard` call.

Usage

```
## S3 method for class 'ddhazard'
residuals(
  object,
  type = c("std_space_error", "space_error", "pearson", "raw"),
  data = NULL,
  ...
)
```

Arguments

object	result of <code>ddhazard</code> call.
type	type of residuals. Four possible values: "std_space_error", "space_error", "pearson" and "raw". See the sections below for details.
data	data.frame with data for the Pearson or raw residuals. This is only needed if the data set is not saved with the object. Must be the same data set used in the initial call to <code>ddhazard</code> .
...	not used.

Value

Returns a list as described in the Pearson and raw residuals section and in the State space errors section.

Pearson and raw residuals

Is the result of a call with a type argument of either "pearson" or "raw" for Pearson residuals or raw residuals. Returns a list with class "ddhazard_residual" with the following elements.

`residuals` list of residuals for each bin. Each element of the list contains a 2D array where the rows corresponds to the passed data and columns are the residuals (`residuals`), estimated probability of death (`p_est`), outcome (`Y`) and row number in the initial data set (`row_num`). The data rows will only have a residuals in a given risk list if they are at risk in that risk set.

`type` the type of residual.

State space errors

Is the result of a call with a type argument of either "std_space_error" or "space_error". The former is for standardized residuals while the latter is non-standardized. Returns a list with class "ddhazard_space_errors" with the following elements:

`residuals` 2D array with either standardized or non-standardized state space errors. The row are bins and the columns are the parameters in the regression.

`standardize` TRUE if standardized state space errors.

`Covariances` 3D array with the smoothed co-variance matrix for each set of the state space errors.

Examples

```
library(dynamichazard)
fit <- ddhazard(
  Surv(time, status == 2) ~ log(bili), pbc, id = pbc$id, max_T = 3600,
  Q_0 = diag(1, 2), Q = diag(1e-4, 2), by = 50,
  control = ddhazard_control(method = "GMA"))
resids <- residuals(fit, type = "pearson")$residuals
head(resids[[1]])
head(resids[[2]])
```

static_glm

Static glm Fit

Description

Method to fit a static model corresponding to a [ddhazard](#) fit. The method uses weights to ease the memory requirements. See [get_survival_case_weights_and_data](#) for details on weights.

The `parallelglm_quick` and `parallelglm_QR` methods are similar to two methods used in `bam` function in the `mgcv` package (see the ``use.chol`` argument or Wood et al. 2015). `parallelglm_QR` is more stable but slower. See Golub (2013) section 5.3 for a comparison of the Cholesky decomposition method and the QR method.

Usage

```

static_glm(
  formula,
  data,
  by,
  max_T,
  ...,
  id,
  family = "logit",
  model = FALSE,
  weights,
  risk_obj = NULL,
  speedglm = FALSE,
  only_coef = FALSE,
  mf,
  method_use = c("glm", "speedglm", "parallelglm_quick", "parallelglm_QR"),
  n_threads = getOption("ddhazard_max_threads")
)

```

Arguments

formula	coxph like formula with <code>Surv(tstart, tstop, event)</code> on the left hand site of <code>~</code> .
data	data.frame or environment containing the outcome and covariates.
by	interval length of the bins in which parameters are fixed.
max_T	end of the last interval interval.
...	arguments passed to <code>glm</code> or <code>speedglm</code> . If <code>only_coef = TRUE</code> then the arguments are passed to <code>glm.control</code> if <code>glm</code> is used.
id	vector of ids for each row of the in the design matrix.
family	"logit", "cloglog", or "exponential" for a static equivalent model of <code>ddhazard</code> .
model	TRUE if you want to save the design matrix used in <code>glm</code> .
weights	weights to use if e.g. a skewed sample is used.
risk_obj	a pre-computed result from a <code>get_risk_obj</code> . Will be used to skip some computations.
speedglm	deprecated.
only_coef	TRUE if only coefficients should be returned. This will only call the <code>speedglm::speedglm.wfit</code> or <code>glm.fit</code> which will be faster.
mf	model matrix for regression. Needed when <code>only_coef = TRUE</code>
method_use	method to use for estimation. <code>glm</code> uses <code>glm.fit</code> , <code>speedglm::speedglm</code> uses <code>speedglm::speedglm.wfit</code> and <code>parallelglm_quick</code> and <code>parallelglm_QR</code> uses a parallel C++ estimation method.
n_threads	number of threads to use when <code>method_use</code> is "parallelglm".

Value

The returned list from the `glm` call or just coefficients depending on the value of `only_coef`.

References

Wood, S.N., Goude, Y. & Shaw S. (2015) Generalized additive models for large datasets. *Journal of the Royal Statistical Society, Series C* 64(1): 139-155.

Golub, G. H., & Van Loan, C. F. (2013). *Matrix computations* (4th ed.). JHU Press.

Examples

```
library(dynamichazard)
fit <- static_glm(
  Surv(time, status == 2) ~ log(bili), pbc, id = pbc$id, max_T = 3600,
  by = 50)
fit$coefficients
```

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