

# Package ‘stagedtrees’

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**Type** Package

**Title** Staged Event Trees

**Version** 2.2.1

**Description** Creates and fits staged event tree probability models, which are probabilistic graphical models capable of representing asymmetric conditional independence statements for categorical variables.

Includes functions to create, plot and fit staged event trees from data, as well as many efficient structure learning algorithms.

References:

Collazo R. A., Görgen C. and Smith J. Q. (2018, ISBN:9781498729604).

Görgen C., Bigatti A., Riccomagno E. and Smith J. Q. (2018) <[arXiv:1705.09457](https://arxiv.org/abs/1705.09457)>.

Thwaites P. A., Smith, J. Q. (2017) <[arXiv:1510.00186](https://arxiv.org/abs/1510.00186)>.

Barclay L. M., Hutton J. L. and Smith J. Q. (2013) <[doi:10.1016/j.ijar.2013.05.006](https://doi.org/10.1016/j.ijar.2013.05.006)>.

Smith J. Q. and Anderson P. E. (2008) <[doi:10.1016/j.artint.2007.05.004](https://doi.org/10.1016/j.artint.2007.05.004)>.

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**NeedsCompilation** no

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---

as.character.parentslist

*Print a parentslist object*

---

## Description

Nice print of a parentslist object

## Usage

```
## S3 method for class 'parentslist'
as.character(x, only_parents = FALSE, ...)
```

```
## S3 method for class 'parentslist'
print(x, ...)
```

## Arguments

`x` an object of class `parentslist`.  
`only_parents` logical, if the basic DAG encoding is to be returned.  
`...` additional arguments for compatibility.

## Value

`as.character.parentslist` returns a string encoding the associated directed graph and eventually the context specific independences. The encoding is similar to the one returned by `modelstring` in package **bnlearn** and package **deal**. In particular, parents of a variable can be enclosed in:

- ( ) if a partial (conditional) independence is present.
- { } if a context specific independence is present.
- <> if no context specific and partial (conditional) independences are present, but at least a local independence is detected.

If a parent is not enclosed in parenthesis the dependence is full.

If `only_parents = TRUE`, the simple DAG encoding as in **bnlearn** is returned.

**Examples**

```

model <- stages_hclust(full(Titanic), k = 2)
pl <- as_parentslist(model)
pl
as.character(pl)
as.character(pl, only_parents = TRUE)

```

---

Asym

*Asym dataset*


---

**Description**

Artificial dataset with observations from four variables having a non-symmetrical conditional independence structure.

**Usage**

```
Asym
```

**Format**

A data frame with 1000 observations of 4 binary variables.

**Source**

The data has been generated by Federico Carli <carli@dim.unige>.

---

as\_adj\_matrix

*Convert to an adjacency matrix*


---

**Description**

Convert to an adjacency matrix

**Usage**

```

as_adj_matrix(x)

## S3 method for class 'parentslist'
as_adj_matrix(x)

```

**Arguments**

x                    an R object

**Value**

the equivalent adjacency matrix

---

as_bn	<i>Convert to a <b>bnlearn</b> object</i>
-------	---

---

### Description

Convert a staged tree object into an object of class bn from the **bnlearn** package.

### Usage

```
as_bn(x)

## S3 method for class 'parentslist'
as_bn(x)

## S3 method for class 'sevt'
as_bn(x)
```

### Arguments

x                    an R object of class sevt or parentslist.

### Value

an object of class bn from package **bnlearn**.

---

as_parentslist	<i>Obtain the equivalent DAG as list of parents</i>
----------------	---

---

### Description

Convert to the equivalent representation as list of parents.

### Usage

```
as_parentslist(x, ...)
```

```
## S3 method for class 'bn'
as_parentslist(x, order = NULL, ...)
```

```
## S3 method for class 'bn.fit'
as_parentslist(x, order = NULL, ...)
```

```
## S3 method for class 'sevt'
as_parentslist(x, ...)
```

**Arguments**

x	an R object.
...	additional parameters.
order	order of the variables, usually a topological order.

**Details**

The output of this function is an object of class `parentslist` which is one of the possible encoding for a directed graph. This is mainly an internal class and its specification can be changed in the future. For example, now it may also include information on the sample space of the variables and the context/partial/local independences.

In `as_parentslist.sevt`, if a context-specific or a local-partial independence is detected a message is printed and the minimal super-model is returned.

**Value**

An object of class `parentslist` for which a print method exists. Basically a list with one entries for each variable with fields:

- `parents` The parents of the variable.
- `context` Where context independences are detected.
- `partial` Where partial independences are detected.
- `local` Where no context/partial independences are detected, but local independences are present.
- `values` values for the variable.

**See Also**

[print.parentslist](#) and [as.character.parentslist](#) for the parenthesis-encoding of the DAG structure and the asymmetric independences.

**Examples**

```
model <- stages_hclust(full(Titanic), k = 2)
pl <- as_parentslist(model)
pl$Age
```

---

as\_sevt

*Coerce to sevt*

---

**Description**

Convert to an equivalent object of class [sevt](#).

## Usage

```
as_sevt(x, ...)  
  
## S3 method for class 'bn.fit'  
as_sevt(x, order = NULL, ...)  
  
## S3 method for class 'bn'  
as_sevt(x, order = NULL, values = NULL, ...)  
  
## S3 method for class 'parentslist'  
as_sevt(x, order = NULL, values = NULL, ...)
```

## Arguments

x	an R object.
...	additional parameters to be used by specific methods.
order	order of the variables.
values	the values for each variable, the sample space.

## Details

In `as_sevt.bn.fit` the `order` argument, if provided, must be a topological order of the `bn.fit` object (no check is performed). If the order is not provided a topological order will be used (the one returned by `bnlearn::node.ordering`).

In `as_sevt.parentslist` the `order` argument, if provided, must be a topological order of the corresponding DAG (no check is performed). If the order is not provided `names(x)` is used.

The `values` parameter is used to specify the sample space of each variable. For a `parentslist` object created with `as_parentslist` from an object of class `sevt`, it is, usually, not needed to specify the `values` parameter, since the sample space is saved in the `parentslist` object.

## Value

the equivalent object of class `sevt`.

## Examples

```
model <- stages_hclust(full(Titanic), k = 2)  
plot(model)  
pl <- as_parentslist(model)  
model2 <- as_sevt(pl)  
plot(model2) ## this is a super-model of the first staged tree  
## we can check it with  
inclusions_stages(model, model2)
```

---

barplot.sevt

*Bar plots of stage probabilities*


---

### Description

Create a bar plot visualizing probabilities associated to the different stages of a variable in a staged event tree.

### Usage

```
## S3 method for class 'sevt'
barplot(
  height,
  var,
  ignore = height$name_unobserved,
  beside = TRUE,
  horiz = FALSE,
  legend.text = FALSE,
  col = NULL,
  xlab = ifelse(horiz, "probability", NA),
  ylab = ifelse(!horiz, "probability", NA),
  ...
)
```

### Arguments

height	an object of class <code>sevt</code> .
var	name of a variable in object.
ignore	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in <code>object\$name_unobserved</code> .
beside	a logical value. See <a href="#">barplot</a> .
horiz	a logical value. See <a href="#">barplot</a> .
legend.text	logical.
col	color mapping for the stages, see <code>col</code> argument in <a href="#">plot.sevt</a> .
xlab	a label for the x axis.
ylab	a label for the y axis.
...	additional arguments passed to <a href="#">barplot</a> .

### Value

As [barplot](#): A numeric vector (or matrix, when `beside = TRUE`), giving the coordinates of all the bar midpoints drawn, useful for adding to the graph.



**Examples**

```
model <- stages_fbhc(full(PhDArticles, lambda = 1))
barplot(model, "Kids", beside = TRUE)
```

---

ceg	<i>Chain event graph (CEG)</i>
-----	--------------------------------

---

**Description**

Build the CEG representation from an object of class `sevt`.

**Usage**

```
ceg(object)
```

**Arguments**

`object` an object of class `sevt`.

**Details**

An object of class `ceg` is a staged event tree object with additional information on the positions.

**Value**

an object of class `ceg`.

**Examples**

```
DD <- generate_xor_dataset(3, 100)
model <- stages_bhc(full(DD))
model.ceg <- ceg(model)
model.ceg$positions
```

---

ceg2adjmat	<i>Ceg to adjmat of graph</i>
------------	-------------------------------

---

**Description**

Obtain the adjacency matrix corresponding to a CEG.

**Usage**

```
ceg2adjmat(x)
```

**Arguments**

x an object of class `ceg`.

**Details**

This utility function can be used to prepare the adjacency matrix to plot the CEG using a graph package (e.g. `igraph`).

**Value**

the adj matrix

**Examples**

```
model <- stages_fbhc(full(PhDArticles))
model.ceg <- ceg(model)
ceg2adjmat(model.ceg)
```

---

 cid

*Context specific interventional discrepancy*


---

**Description**

Compute the context specific interventional discrepancy of a staged tree with respect to a reference staged tree.

**Usage**

```
cid(object1, object2, FUN = mean)
```

**Arguments**

object1 an object of class `sevt`.

object2 an object of class `sevt`.

FUN a function that is used to aggregate CID for each variable. The default mean will obtain the CID as defined in Leonelli and Varando (2021).

**Value**

A list with components:

- `wrong` a stages-like structure which record where `object2` wrongly infer the interventional distance with respect to `object1`.
- `cid` the value of the computed CID.

## References

Leonelli M., Varando G. Context-Specific Causal Discovery for Categorical Data Using Staged Trees <https://arxiv.org/abs/2106.04416>

## Examples

```
model1 <- stages_bhc(full(Titanic))
model2 <- stages_bhc(full(Titanic,
                          order = c("Survived", "Sex", "Age", "Class")))
cid(model1, model2)$cid
cid(model1, model2)$wrong
```

---

compare_stages	<i>Compare two staged event tree</i>
----------------	--------------------------------------

---

## Description

Compare two staged event trees, return the differences of the stages structure and plot the difference tree. Three different methods to compute the difference tree are available (see Details).

## Usage

```
compare_stages(
  object1,
  object2,
  method = "naive",
  return_tree = FALSE,
  plot = FALSE,
  ...
)

hamming_stages(object1, object2, return_tree = FALSE)

diff_stages(object1, object2)
```

## Arguments

object1	an object of class <code>sevt</code> .
object2	an object of class <code>sevt</code> .
method	character, method to compare staged event trees. One of: "naive", "hamming" or "stages".
return_tree	logical, if TRUE the difference tree is returned.
plot	logical.
...	additional parameters to be passed to <code>plot.sevt</code> .

## Details

compare\_stages tests if the stage structure of two sevt objects is the same. Three methods are available:

- naive first applies `stndnaming` to both objects and then simply compares the resulting stage names.
- hamming uses the `hamming_stages` function that finds a minimal subset of nodes which stages must be changed to obtain the same structure.
- stages uses the `diff_stages` function that compares stages to check whether the same stage structure is present in both models.

Setting `return_tree = TRUE` will return the stages difference obtained with the selected method. The stages difference is a list of numerical vectors with same lengths and structure as `stages(object1)` or `stages(object2)`, where values are 1 if the corresponding node has different (with respect to the selected method) associated stage, and 0 otherwise.

With `plot = TRUE` the plot of the difference tree is displayed.

If `return_tree = FALSE` and `plot = FALSE` the logical output is the same for the three methods and thus the naive method should be used since it is computationally faster.

`hamming_stages` finds a minimal set of nodes for which the associated stages should be changed to obtain equivalent structures. To do that, a maximum-weight bipartite matching problem between the stages of the two staged trees is solved using the Hungarian method implemented in the `solve_LSAP` function of the **clue** package. `hamming_stages` requires the package `clue`.

## Value

`compare_stages`: if `return_tree = FALSE`, logical: TRUE if the two models are exactly equal, otherwise FALSE. Else if `return_tree = TRUE`, the differences between the two trees, according to the selected method.

`hamming_stages`: if `return_tree = FALSE`, integer, the minimum number of situations where the stage should be changed to obtain the same models. If `return_tree = TRUE` a stages-like structure showing which situations should be modified to obtain the same models.

`diff_stages`: a stages-like structure marking the situations belonging to stages which are not the exactly equal.

## Examples

```
data("Asym")
mod1 <- stages_bhc(full(Asym, lambda = 1))
mod2 <- stages_fbhc(full(Asym, lambda = 1))
compare_stages(mod1, mod2)

#####
m0 <- full(PhDArticles[, 1:4], lambda = 0)
m1 <- stages_bhc(m0)
m2 <- stages_bj(m0, distance = "totvar", thr = 0.25)
diff_stages(m1, m2)
```

---

confint.sevt                      *Confidence intervals for staged event tree parameters*

---

## Description

Confint method for class sevt.

## Usage

```
## S3 method for class 'sevt'
confint(
  object,
  parm,
  level = 0.95,
  method = c("wald", "waldcc", "wilson", "goodman", "quesenberry-hurst"),
  ignore = object$name_unobserved,
  ...
)
```

## Arguments

object	an object of class sevt.
parm	a specification of which parameters are to be given confidence intervals, either a vector of numbers or a vector of names. If missing, all parameters are considered.
level	the confidence level required.
method	a character string specifying which method to use: "wald", "waldcc", "goodman", "quesenberry-hurst" or "wilson".
ignore	vector of stages which will be ignored, by default the name of the unobserved stages stored in object\$name_unobserved.
...	additional argument(s) for compatibility with confint methods.

## Details

Compute confidence intervals for staged event trees. Currently five methods are available:

- wald, waldcc: Wald method and with continuity correction.
- wilson, quesenberry-hurst and goodman.

## Value

A matrix with columns giving lower and upper confidence limits for each parameter. These will be labelled as  $(1-level)/2$  and  $1 - (1-level)/2$  in % (by default 2.5% and 97.5%).

**Author(s)**

The function is partially inspired by code in the `MultinomCI` function from the **DescTools** package, implemented by Andri Signorelli and Pablo J. Villacorta Iglesias.

**References**

- Goodman, L. A. (1965) On Simultaneous Confidence Intervals for Multinomial Proportions *Technometrics*, 7, 247-254.
- Wald, A. Tests of statistical hypotheses concerning several parameters when the number of observations is large, *Trans. Am. Math. Soc.* 54 (1943) 426-482.
- Wilson, E. B. Probable inference, the law of succession and statistical inference, *J. Am. Stat. Assoc.* 22 (1927) 209-212.
- Quesenberry, C., & Hurst, D. (1964). Large Sample Simultaneous Confidence Intervals for Multinomial Proportions. *Technometrics*, 6(2), 191-195

**Examples**

```
m1 <- stages_bj(full(PhDArticles), distance = "kullback", thr = 0.01)
confint(m1, "Prestige", level = 0.90)
confint(m1, "Married", method = "goodman")
confint(m1, c("Married", "Kids"))
```

---

full\_indep

*Full and independent staged event tree*


---

**Description**

Build fitted staged event tree from data.

**Usage**

```
full(
  data,
  order = NULL,
  join_unobserved = TRUE,
  lambda = 0,
  name_unobserved = "UNOBSERVED"
)

## S3 method for class 'table'
full(
  data,
  order = names(dimnames(data)),
  join_unobserved = TRUE,
  lambda = 0,
  name_unobserved = "UNOBSERVED"
```

```
)

## S3 method for class 'data.frame'
full(
  data,
  order = colnames(data),
  join_unobserved = TRUE,
  lambda = 0,
  name_unobserved = "UNOBSERVED"
)

indep(
  data,
  order = NULL,
  join_unobserved = TRUE,
  lambda = 0,
  name_unobserved = "UNOBSERVED"
)

## S3 method for class 'table'
indep(
  data,
  order = names(dimnames(data)),
  join_unobserved = TRUE,
  lambda = 0,
  name_unobserved = "UNOBSERVED"
)

## S3 method for class 'data.frame'
indep(
  data,
  order = colnames(data),
  join_unobserved = TRUE,
  lambda = 0,
  name_unobserved = "UNOBSERVED"
)
```

### Arguments

data	data to create the model, data.frame or table.
order	character vector, order of variables.
join_unobserved	logical, if situations with zero observations should be joined (default TRUE).
lambda	smoothing coefficient (default 0).
name_unobserved	name to pass to <a href="#">join_unobserved</a> .

**Details**

Functions to create full or independent staged tree models from data. The full (or saturated) staged tree is the model where every situation is in a different stage, and thus the model has the maximum number of parameters. Conversely, the independent staged tree (`indep`) assigns all the situations related to the same variable to the same stage, thus it is equivalent to the independence factorization.

**Examples**

```
## full model
DD <- generate_xor_dataset(4, 100)
model_full <- full(DD, lambda = 1)

## independence model (data.frame)
DD <- generate_xor_dataset(4, 100)
model <- indep(DD, lambda = 1)
model
```

---

```
generate_linear_dataset
```

*Generate a random binary dataset for classification*

---

**Description**

Randomly generate a simple classification problem.

**Usage**

```
generate_linear_dataset(
  n = 2,
  N = 10000,
  eps = 1.2,
  gamma = runif(1, min = -n, max = n),
  alpha = runif(n, min = -n, max = n)
)
```

**Arguments**

<code>n</code>	number of variables.
<code>N</code>	number of observations.
<code>eps</code>	noise.
<code>gamma</code>	numeric.
<code>alpha</code>	numeric vector of length <code>n</code> .

**Value**

A data.frame with `n` independent random variables and one class variable `C` computed as  $\text{sign}(\sum(x * \alpha) + \text{runif}(1, -\text{eps}, \text{eps}) + \text{gamma})$ .



**Examples**

```
DD <- generate_linear_dataset(n = 5, 1000)
```

---

```
generate_random_dataset
```

*Generate a random binary dataset*

---

**Description**

Randomly generate a data.frame of independent binary variables.

**Usage**

```
generate_random_dataset(n = 2, N = 10000)
```

**Arguments**

n	number of variables.
N	number of observations.

**Value**

A data.frame with n independent random variables.

**Examples**

```
DD <- generate_random_dataset(n = 5, 1000)
```

---

```
generate_xor_dataset
```

*Generate a xor dataset*

---

**Description**

Generate a xor dataset

**Usage**

```
generate_xor_dataset(n = 2, N = 100, eps = 1.2)
```

**Arguments**

n	number of variables.
N	number of observations.
eps	error.

**Value**

The xor dataset with  $n + 1$  variables, where the first one is the class variable  $C$  computed as a noisy xor.

**Examples**

```
DD <- generate_xor_dataset(n = 5, N = 1000, eps = 1.2)
```

---

<code>get_stage</code>	<i>Get stage or path</i>
------------------------	--------------------------

---

**Description**

Utility functions to obtain stages from paths and paths from stages.

**Usage**

```
get_stage(object, path)
```

```
get_path(object, var, stage)
```

**Arguments**

<code>object</code>	an object of class <code>sevt</code> .
<code>path</code>	character vector, the path from root or a two dimensional array where each row is a path from root.
<code>var</code>	character, one of the variable in the staged tree.
<code>stage</code>	character vector, the name of the stages for which the paths should be returned.

**Value**

`get_stage` returns the stage name(s) for given path(s).

`get_path` returns a data.frame containing the paths corresponding to the given stage(s).

**Examples**

```
model <- stages_fbhc(full(PhDArticles))
get_stage(model, c("0", "male"))
paths <- expand.grid(model$tree[2:1])[, 2:1]
get_stage(model, paths)
get_path(model, "Kids", "5")
get_path(model, "Gender", "2")
get_path(model, "Kids", c("5", "6"))
```

---

inclusions_stages	<i>Inclusions of stages</i>
-------------------	-----------------------------

---

**Description**

Display the relationship between two staged tree models over the same variables.

**Usage**

```
inclusions_stages(object1, object2)
```

**Arguments**

object1	an object of class sevt.
object2	an object of class sevt.

**Details**

Computes the relations between the stages structures of the two models.

The relations between stages of the same variable are stored in a data frame with three columns where each row represent a relation between a stage of the first model (s1) and a stage of the second model (s2). The relation can be one of the following: inclusion ( $s1 < s2$  or  $s1 > s2$ ; equal ( $s1 = s2$ ); not-equal ( $s1 \neq s2$ ).

**Value**

a list with inclusion relations between stage structures for each variable in the models.

**Examples**

```
mod1 <- stages_bhc(full(PhDArticles[, 1:5], lambda = 1))
mod2 <- stages_fbhc(full(PhDArticles[, 1:5], lambda = 1))
inclusions_stages(mod1, mod2)
```

---

join_stages	<i>Join stages</i>
-------------	--------------------

---

**Description**

Join two stages in a staged event tree object, updating probabilities and log-likelihood accordingly.

**Usage**

```
join_stages(object, v, s1, s2)
```

**Arguments**

object	an object of class sevt.
v	variable.
s1	first stage.
s2	second stage.

**Details**

This function joins two stages associated to the same variable, updating probabilities and log-likelihood if the object was fitted.

**Value**

the staged event tree where s1 and s2 are joined.

**Examples**

```
model <- full(PhDArticles, lambda = 0)
model <- stages_fbhc(model)
model$stages$Kids
model <- join_stages(model, "Kids", "5", "6")
model$stages$Kids
```

---

join\_unobserved

*Join situations with no observations*

---

**Description**

Join situations with no observations

**Usage**

```
join_unobserved(
  object,
  fit = TRUE,
  trace = 0,
  name = "UNOBSERVED",
  scope = sevt_varnames(object)[-1],
  lambda = object$lambda
)
```

**Arguments**

object	an object of class sevt with associated data.
fit	if TRUE update model's probabilities.
trace	if > 0 print information to console.
name	character, name for the new stage storing unobserved situations.
scope	character vector, list of variables in object.
lambda	smoothing parameter for the fitting.

**Details**

It takes as input a (fitted) staged event tree object and it joins, in the same stage, all the situations with zero recorded observations. Since such joining does not change the log-likelihood of the model, it is a useful (time-wise) pre-processing prior to others model selection algorithms.

Unobserved situations can be joined directly in `full` or `indep`, by setting `join_unobserved = TRUE`.

**Value**

a staged event tree with at most one stage per variable with no observations. If, as default, `fit=TRUE` the model will be re-fitted, if `fit=FALSE` probabilities in the output model are not estimated.

**Examples**

```
DD <- generate_xor_dataset(n = 5, N = 10)
model_full <- full(DD, lambda = 1, join_unobserved = FALSE)
model <- join_unobserved(model_full)
logLik(model_full)
logLik(model)
BIC(model_full, model)
```

---

logLik.sevt

*Log-Likelihood of a staged event tree*


---

**Description**

Compute, or extract the log-likelihood of a staged event tree.

**Usage**

```
## S3 method for class 'sevt'
logLik(object, ...)
```

**Arguments**

object	an fitted object of class sevt.
...	additional parameters (compatibility).

**Value**

An object of class `logLik`.

**Examples**

```
data("PhDArticles")
mod <- indep(PhDArticles)
logLik(mod)
```

---

 lr\_test

*Likelihood Ratio Test for staged trees models*


---

**Description**

Function to perform likelihood ratio test between two or multiple staged event tree models.

**Usage**

```
lr_test(object, ...)
```

**Arguments**

<code>object</code>	an object of class <code>sevt</code> .
<code>...</code>	further objects of class <code>sevt</code> . Must specify super-models of <code>object</code> . See below for details.

**Details**

If a single object of class `sevt` is passed as argument, it computes the likelihood-ratio test with respect to the independence model. If multiple objects are passed, likelihood-ratio tests between the first object and the followings are computed. In the latter casem the function checks automatically if the first model is nested in the additional ones, via `inclusions_stages`, and throws an error if not.

**Value**

An object of class `anova` which contains the log-likelihood, degrees of freedom, difference in degrees of freedom, likelihood ratio statistics and corresponding p values.

**Examples**

```
data(PhDArticles)
order <- c("Gender", "Kids", "Married", "Articles")
phd.mod1 <- stages_hc(indep(PhDArticles, order))
phd.mod2 <- stages_hc(full(PhDArticles, order))

## compare two nested models
lr_test(phd.mod1, phd.mod2)
```

```
## compare a single model vs the independence model  
lr_test(phd.mod1)
```

---

PhDArticles

*PhD Students Publications*

---

### Description

Number of publications of 915 PhD biochemistry students during the 1950's and 1960's.

### Usage

PhDArticles

### Format

A data frame with 915 rows and 6 variables:

**Articles** Number of articles during the last 3 years of PhD: either 0, 1-2 or >2.

**Gender** male or female.

**Kids** yes if the student has at least one kid 5 or younger, no otherwise.

**Married** yes or no.

**Mentor** Number of publications of the student's mentor: low between 0 and 3, medium between 4 and 10, high otherwise.

**Prestige** low if the student is at a low-prestige university, high otherwise.

### Source

The data has been modified from the Rchoice package.

### References

Long, J. S. (1990). The origins of sex differences in science. *Social Forces*, 68(4), 1297-1316.

---

plot.ceg

*igraph's plotting for CEG*


---

## Description

igraph's plotting for CEG

## Usage

```
## S3 method for class 'ceg'
plot(x, col = NULL, ignore = x$name_unobserved, layout = NULL, ...)
```

## Arguments

x	an object of class <a href="#">ceg</a> .
col	colors specification see <a href="#">plot.sevt</a> .
ignore	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in <code>x\$name_unobserved</code> .
layout	an igraph layout.
...	additional arguments passed to <code>plot.igraph</code> .

## Details

This function is a simple wrapper around **igraph's** `plot.igraph`. The `ceg` object is converted to an `igraph` object by firstly obtaining the adjacency matrix representation with [ceg2adjmat](#). If not specified, the default layout used is a rotated `layout.reingold.tilford`.

We use `palette()` as palette for the **igraph** plotting, while `plot.igraph` uses as default a different palette. This is to allow matching stages colors between `plot.ceg` and [plot.sevt](#).

## Examples

```
## Not run:
model <- stages_bhc(full(Titanic))
model.ceg <- ceg(model)
plot(model.ceg, edge.arrow.size = 0.1, vertex.label.dist = -2)

## End(Not run)
```



---

plot.sevt                      *Plot method for staged event trees*

---

### Description

Plot method for staged event tree objects. It allows easy plotting of staged event trees with some options (see Examples).

### Usage

```
## S3 method for class 'sevt'  
plot(  
  x,  
  y = 10,  
  limit = y,  
  xlim = c(0, 1),  
  ylim = c(0, 1),  
  main = NULL,  
  sub = NULL,  
  asp = 1,  
  cex_label_nodes = 0,  
  cex_label_edges = 1,  
  cex_nodes = 2,  
  cex_tree_y = 0.9,  
  col = NULL,  
  col_edges = "black",  
  var_names = TRUE,  
  ignore = x$name_unobserved,  
  pch_nodes = 16,  
  lwd_nodes = 1,  
  lwd_edges = 1,  
  ...  
)  
  
make_stages_col(x, col = NULL, ignore = x$name_unobserved, limit = NULL)
```

### Arguments

x	an object of class sevt.
y	alias for limit for compatibility with plot.
limit	maximum number of variables plotted.
xlim	the x limits (x1, x2) of the plot.
ylim	the y limits of the plot.
main	an overall title for the plot.
sub	a sub title for the plot.

asp	the y/x aspect ratio.
cex_label_nodes	the magnification to be used for the node labels. If set to 0 (as default) node labels are not showed.
cex_label_edges	the magnification for the edge labels. If set to 0 edge labels are not displayed.
cex_nodes	the magnification for the nodes of the tree.
cex_tree_y	the magnification for the tree in the vertical direction. Default is 0.9 to leave some space for the variable names.
col	color mapping for stages, one of the following: NULL (color will be assigned based on the current palette); a named (variables) list of named (stages) vectors of colors; the character "stages", in which case the stage names will be used as colors; a function that takes as input a vector of stages and output the corresponding colors. Check the provided examples. The function <code>make_stages_col</code> is used internally and <code>make_stages_col(x, NULL)</code> or <code>make_stages_col(x, "stages")</code> can be used as a starting point for colors tweaking.
col_edges	color for the edges.
var_names	logical, if variable names should be added to the plot, otherwise variable names can be added manually using <code>text.sevt</code> .
ignore	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in <code>x\$name_unobserved</code> .
pch_nodes	either an integer specifying a symbol or a single character to be used as the default in plotting nodes shapes see <code>points</code> .
lwd_nodes	the line width for edges, a positive number, defaulting to 1.
lwd_edges	the line width for nodes, a positive number, defaulting to 1.
...	additional graphical parameters to be passed to <code>points</code> , <code>lines</code> , <code>title</code> , <code>text</code> and <code>plot.window</code> .

## Examples

```

data("PhDArticles")
mod <- stages_bj(full(PhDArticles, join_unobserved = TRUE))

### simple plotting
plot(mod)

### labels in nodes
plot(mod, cex_label_nodes = 1, cex_nodes = 0)

### reduce nodes size
plot(mod, cex_nodes = 0.5)

### change line width and nodes style
plot(mod, lwd_edges = 3, pch_nodes = 5)

### changing palette

```

```

plot(mod, col = function(s) heat.colors(length(s)))

### or changing global palette
palette(hcl.colors(10, "Harmonic"))
plot(mod)
palette("default") ##

### forcing plotting of unobserved stages
plot(mod, ignore = NULL)

### use function to specify colors
plot(mod, col = function(stages){
  hcl.colors(n = length(stages))
})

### manually give stages colors
### as an example we will assign colors only to the stages of two variables
### Gender (one stage named "1") and Mentor (six stages)
col <- list(Gender = c("1" = "blue"),
           Mentor = c("UNOBSERVED" = "grey",
                    "2" = "red",
                    "3" = "purple",
                    "10" = "pink",
                    "18" = "green",
                    "22" = "brown"))

### by setting ignore = NULL we will plot also the UNOBSERVED stage for Mentor
plot(mod, col = col, ignore = NULL)

```

---

Pokemon

*Pokemon Go Users*

---

## Description

Demographic information of a population of possible Pokemon Go users.

## Usage

Pokemon

## Format

A data frame with 999 rows and 5 variables:

**Use** Y if the individual used the app, N otherwise

**Age** >30 if the individual is older than 30, <=30 otherwise

**Degree** Yes if the individual completed a Higher Education degree, No otherwise

**Gender** Male or Female

**Activity** Yes if the individual was physically active (i.e. had a walk longer than 30 mins, went for a run or had a bike ride to get some exercise) in the past week before the experiment, No otherwise

**Source**

<https://osf.io/xy5g6/>

**References**

Gabbiadini, Alessandro, Christina Sagioglou, and Tobias Greitemeyer. "Does Pokémon Go lead to a more physically active life style?." *Computers in Human Behavior* 84 (2018): 258-263.

---

predict.sevt	<i>Predict method for staged event tree</i>
--------------	---

---

**Description**

Predict class values from a staged event tree model.

**Usage**

```
## S3 method for class 'sevt'
predict(object, newdata = NULL, class = NULL, prob = FALSE, log = FALSE, ...)
```

**Arguments**

object	an object of class sevt with fitted probabilities.
newdata	the newdata to perform predictions
class	character, the name of the variable to use as the class variable, if NULL the first element names(object\$tree) will be used.
prob	logical, if TRUE the probabilities of class are returned
log	logical, if TRUE log-probabilities are returned
...	additional parameters, see details

**Details**

Predict the most probable a posterior value for the class variable given all the other variables in the model. Ties are broken at random and if, for a given vector of predictor variables, all conditional probabilities are 0, NA is returned.

if prob = TRUE, a matrix with number of rows equals to the number of rows in the newdata and number of columns as the number of levels of the class variable is returned. if log = TRUE, log-probabilities are returned.

if prob = FALSE, a vector of length as the number of rows in the newdata with the level with higher estimated probability for each new observations is returned.

**Value**

A vector of predictions or the corresponding matrix of probabilities.

**Examples**

```

DD <- generate_xor_dataset(n = 4, 600)
order <- c("C", "X1", "X2", "X3", "X4")
train <- DD[1:500, order]
test <- DD[501:600, order]
model <- full(train)
model <- stages_bhc(model)
pr <- predict(model, newdata = test, class = "C")
table(pr, test$C)
# class values:
predict(model, newdata = test, class = "C")
# probabilities:
predict(model, newdata = test, class = "C", prob = TRUE)
# log-probabilities:
predict(model, newdata = test, class = "C", prob = TRUE, log = TRUE)

```

---

print.sevt

---

*Print a staged event tree*


---

**Description**

Print a staged event tree

**Usage**

```

## S3 method for class 'sevt'
print(x, ...)

```

**Arguments**

x                    an object of class sevt.  
...                    additional parameters (compatibility).

**Details**

The order of the variables in the staged tree is printed (from root). In addition the number of levels of each variable is shown in square brackets. If available the log-likelihood of the model is printed.

**Value**

An invisible copy of x.

**Examples**

```

DD <- generate_xor_dataset(5, 100)
model <- full(DD, lambda = 1)
print(model)

```

---

prob	<i>Probabilities for a staged event tree</i>
------	--

---

**Description**

Compute (marginal and/or conditional) probabilities of elementary events with respect to the probability encoded in a staged event tree.

**Usage**

```
prob(object, x, conditional_on = NULL, log = FALSE, na0 = TRUE)
```

**Arguments**

object	an object of class <code>sevt</code> with probabilities.
x	the vector or <code>data.frame</code> of observations.
conditional_on	named vector, the conditioning event.
log	logical, if TRUE log-probabilities are returned.
na0	logical, if NA should be converted to 0.

**Details**

Computes probabilities related to a vector or a `data.frame` of observations.

Optionally, conditional probabilities can be obtained by specifying the conditioning event in `conditional_on`. This can be done either with a single named vector or with a `data.frame` object with the same number of rows of `x`. In the former, the same conditioning is used for all the computed probabilities (if `x` has multiple rows); while with the latter different conditioning events (but on the same variables) can be specified for each row of `x`.

**Value**

the probabilities to observe each observation in `x`, possibly conditional on the event(s) in `conditional_on`.

**Examples**

```
data(Titanic)
model <- full(Titanic, lambda = 1)
samples <- expand.grid(model$tree[c(1, 4)])
pr <- prob(model, samples)
## probabilities sum up to one
sum(pr)
## print observations with probabilities
print(cbind(samples, probability = pr))

## compute one probability
prob(model, c(Class = "1st", Survived = "Yes"))
```

```
## compute conditional probability
prob(model, c(Survived = "Yes"), conditional_on = c(Class = "1st"))

## compute conditional probabilities with different conditioning set
prob(model, data.frame(Age = rep("Adult", 8)),
      conditional_on = expand.grid(model$tree[2:1]))
## the above should be the same as
summary(model)$stages.info$Age
```

---

rename_stage	<i>Rename stage(s) in staged event tree</i>
--------------	---

---

### Description

Change the name of a stage in a staged event tree.

### Usage

```
rename_stage(object, var, stage, new)
```

### Arguments

object	an object of class sevt.
var	name of a variable in object.
stage	name of the stage to be renamed.
new	new name for the stage.

### Details

No internal checks are performed and as side effect stages can be joined, if e.g. new is equal to the name of a stage for variable var.

### Value

a staged event tree object where stages stage have been renamed to new.

---

sample_from	<i>Sample from a staged event tree</i>
-------------	--

---

**Description**

Generate a random sample from the distribution encoded in a staged event tree object.

**Usage**

```
sample_from(object, nsim = 1, seed = NULL)
```

**Arguments**

object	an object of class sevt with fitted probabilities.
nsim	number of observations to sample.
seed	an object specifying if and how the random number generator should be initialized ('seeded'). Either NULL or an integer that will be used in a call to set.seed.

**Details**

It samples nsim observations according to the transition probabilities (object\$prob) in the model.

**Value**

A data frame containing nsim observations from the variables in object.

**Examples**

```
model <- stages_fbhc(full(PhDArticles, lambda = 1))
sample_from(model, 10)
```

---

search_best	<i>Optimal Order Search</i>
-------------	-----------------------------

---

**Description**

Find the optimal staged event tree with a dynamic programming approach.

**Usage**

```
search_best(
  data,
  alg = stages_bhc,
  search_criterion = BIC,
  lambda = 0,
  join_unobserved = TRUE,
  ...
)
```



**Arguments**

data	either a data.frame or a table containing the data.
alg	a function that performs stages structure estimation. Similar to <a href="#">stages_bhc</a> or <a href="#">stages_hclust</a> . The function alg must accept the argument scope.
search_criterion	the criterion minimized in the order search.
lambda	numerical value passed to <a href="#">full</a> .
join_unobserved	logical, passed to <a href="#">full</a> .
...	additional arguments, passed to alg.

**Details**

This function is an implementation of the dynamic programming approach of Silander and Leong (2013). If the search\_criterion is decomposable the returned model attains the best value among all possible orders.

**Value**

The estimated staged event tree model.

**References**

Silander T., Leong TY. A Dynamic Programming Algorithm for Learning Chain Event Graphs. In: Fürnkranz J., Hüllermeier E., Higuchi T. (eds) Discovery Science. DS 2013. *Lecture Notes in Computer Science*, vol 8140. Springer, Berlin, Heidelberg. 2013.

Cowell R and Smith J. Causal discovery through MAP selection of stratified chain event graphs. *Electronic Journal of Statistics*, 8(1):965–997, 2014.

**Examples**

```
## default search using BIC score
model <- search_best(Titanic, alg = stages_kmeans)

## use df as search_criterion
model1 <- search_best(Titanic, alg = stages_bhc,
                      search_criterion = function(m) attr(logLik(m), "df"))
```

---

search\_greedy

*Greedy Order Search*


---

**Description**

Search the optimal staged event tree with a greedy heuristic.

## Usage

```
search_greedy(  
  data,  
  alg = stages_bhc,  
  search_criterion = BIC,  
  lambda = 0,  
  join_unobserved = TRUE,  
  ...  
)
```

## Arguments

<code>data</code>	either a <code>data.frame</code> or a table containing the data.
<code>alg</code>	a function that performs stages structure estimation. Similar to <a href="#">stages_bhc</a> or <a href="#">stages_hclust</a> . The function <code>alg</code> must accept the argument <code>scope</code> .
<code>search_criterion</code>	the criterion minimized in the order search.
<code>lambda</code>	numerical value passed to <a href="#">full</a> .
<code>join_unobserved</code>	logical, passed to <a href="#">full</a> .
<code>...</code>	additional arguments, passed to <code>alg</code> .

## Details

The greedy approach implemented in this function iteratively adds variables to the staged tree that better improve the `search_criterion`.

## Value

The estimated staged event tree model.

## Examples

```
model <- search_greedy(Titanic, alg = stages_fbhc)  
print(model)
```

---

sevt

*Staged event tree (sevt) class*

---

## Description

Structure and usage of S3 class `sevt`, used to store a staged event tree.

**Usage**

```
sevt(x, full = FALSE, order = NULL)

## S3 method for class 'table'
sevt(x, full = FALSE, order = names(dimnames(x)))

## S3 method for class 'data.frame'
sevt(x, full = FALSE, order = colnames(x))

## S3 method for class 'list'
sevt(x, full = FALSE, order = names(x))
```

**Arguments**

x	a list, a data frame or table object.
full	logical, if TRUE the full model is created otherwise the independence model.
order	character vector, order of the variables to build the tree, by default the order of the variables in x.

**Details**

A staged event tree object is a list with components:

- tree (required): A named list with one component for each variable in the model, a character vector with the names of the levels for that variable. The order of the variables in tree is the order of the event tree.
- stages (required): A named list with one component for each variable but the first, a character vector storing the stages for the situations related to path ending in that variable.
- ctables: A named list with one component for each variable, the flat contingency table of that variable given the previous variables.
- lambda: The smoothing parameter used to compute probabilities.
- name\_unobserved: The stage name for unobserved situations.
- prob: The conditional probability tables for every variable and stage. Stored in a named list with one component for each variable, a list with one component for each stage.
- ll: The log-likelihood of the estimated model. If present, `logLik.sevt` will return this value instead of computing the log-likelihood.

The tree structure is never defined explicitly, instead it is implicitly defined by the list tree containing the order of the variables and the names of their levels. This is sufficient to define a complete symmetric tree where an internal node at a depth related to a variable  $v$  has a number of children equal to the cardinality of the levels of  $v$ . The stages information is instead stored as a list of vectors, where each vector is indexed as the internal nodes of the tree at a given depth.

To define a staged tree from data (data frame or table) the user can call either `full` or `indep` which both construct the staged tree object, attach the data in `ctables` and compute probabilities. After, one of the available model selection algorithm can be used, see for example `stages_hc`, `stages_bhc` or `stages_hclust`. If, mainly for development, only the staged tree structure is needed (without data or probabilities) the basic `sevt` constructor can be used.

**Value**

A staged event tree object, an object of class `sevt`.

**Examples**

```
##### from table
model.titanic <- sevt(Titanic, full = TRUE)

##### from data frame
DD <- generate_random_dataset(n = 4, 1000)
model.indep <- sevt(DD)
model.full <- sevt(DD, full = TRUE)

##### from list
model <- sevt(list(
  X = c("good", "bad"),
  Y = c("high", "low")
))
```

---

`sevt_add`*Add a variable to a staged event tree*

---

**Description**

Return an updated staged event tree with one additional variable at the end of the tree.

**Usage**

```
sevt_add(object, var, data, join_unobserved = TRUE)
```

**Arguments**

<code>object</code>	an object of class <code>sevt</code> .
<code>var</code>	character, the name of the new variable to be added.
<code>data</code>	either a <code>data.frame</code> or a <code>table</code> containing the data from the variables in <code>object</code> plus <code>var</code> .
<code>join_unobserved</code>	logical, passed to <code>full</code> .

**Details**

This function update a staged event tree object with an additional variable. The stages structure of the new variable is initialized as in the saturated model.

**Value**

An object of class `sevt` representing a staged event tree model with `var` added as last variable.

**Examples**

```

model <- full(Titanic, order = c("Age", "Class"))
print(model)
model <- sevt_add(model, "Survived", Titanic)
print(model)

```

sevt\_fit

*Fit a staged event tree***Description**

Estimate transition probabilities in a staged event tree from data. Probabilities are estimated with the relative frequencies plus, eventually, an additive (Laplace) smoothing.

**Usage**

```
sevt_fit(object, data = NULL, lambda = object$lambda)
```

**Arguments**

object	an object of class sevt.
data	data.frame or contingency table with observations of the variables in object.
lambda	smoothing parameter or pseudocount.

**Details**

The data in form of contingency tables and the log-likelihood of the model is stored in the returned staged event tree.

**Value**

A fitted staged event tree, that is an object of class sevt with ctables, prob and ll components.

**Examples**

```

#####
model <- sevt(list(
  X = c("good", "bad"),
  Y = c("high", "low")
))
D <- data.frame(
  X = c("good", "good", "bad"),
  Y = c("high", "low", "low")
)
model.fit <- sevt_fit(model, data = D, lambda = 1)

```

---

stagedtrees

*Staged event trees.*

---

## Description

Algorithms to create, learn, fit and explore staged event tree models. Functions to compute probabilities, make predictions from the fitted models and to plot, analyze and manipulate staged event trees.

## Details

A staged event tree is a representation of a particular factorization of a joint probability over a product space. In particular, given a vector of categorical random variables  $X_1, X_2, \dots$ , a staged event tree represents the factorization  $P(X_1, X_2, X_3, \dots) = P(X_1)P(X_2|X_1)P(X_3|X_1, X_2) \dots$ . Additionally, the stages structure indicates which conditional probabilities are equal.

Model selection algorithms:

- full model [full](#)
- independence model [indep](#)
- Hill-Climbing [stages\\_hc](#)
- Backward Hill-Climbing [stages\\_bhc](#)
- Fast Backward Hill-Climbing [stages\\_fbhc](#)
- Backward Hill-Climbing Random [stages\\_bhcr](#)
- Backward joining [stages\\_bj](#)
- Hierarchical Clustering [stages\\_hclust](#)
- K-Means Clustering [stages\\_kmeans](#)
- Optimal order search [search\\_best](#)
- Greedy order search [search\\_greedy](#)

Probabilities, log-likelihood and predictions:

- Marginal/Conditional probabilities [prob](#)
- Log-Likelihood [logLik.sevt](#)
- Predict method [predict.sevt](#)
- Confidence intervals [confint.sevt](#)

Plot, explore and compare:

- Plot [plot.sevt](#)
- Compare [compare\\_stages](#)
- Stages inclusion [inclusions\\_stages](#)
- Stages info [summary.sevt](#)
- List of parents [as\\_parentslist](#)

- Barplot construction [barplot.sevt](#)
- Likelihood-ratio test [lr\\_test](#)
- Context-specific interventional distance [cid](#)

Modify models:

- Join and isolate unobserved situations [join\\_unobserved](#)
- Join two stages [join\\_stages](#)
- Rename a stage [rename\\_stage](#)

## References

Collazo R. A., Görden C. and Smith J. Q. Chain event graphs. CRC Press, 2018.

Görden C., Bigatti A., Riccomagno E. and Smith J. Q. Discovery of statistical equivalence classes using computer algebra. *International Journal of Approximate Reasoning*, vol. 95, pp. 167-184, 2018.

Barclay L. M., Hutton J. L. and Smith J. Q. Refining a Bayesian network using a chain event graph. *International Journal of Approximate Reasoning*, vol. 54, pp. 1300-1309, 2013.

Smith J. Q. and Anderson P. E. Conditional independence and chain event graphs. *Artificial Intelligence*, vol. 172, pp. 42-68, 2008.

Thwaites P. A., Smith, J. Q. A new method for tackling asymmetric decision problems. *International Journal of Approximate Reasoning*, vol. 88, pp. 624–639, 2017.

## Examples

```
data("PhDArticles")
mf <- full(PhDArticles, join_unobserved = TRUE)
mod <- stages_fbhc(mf)
plot(mod)
```

---

stages

*Stages of a variable*

---

## Description

Obtain the stages of a given variable in a staged event tree object.

## Usage

```
stages(object, var = NULL)
```

## Arguments

object	an object of class <code>sevt</code> .
var	name of one variable in object.

**Value**

If `var` is specified, it returns a character vector with stage names for the given variable (that is `object$stages[[var]]`). Otherwise, If `var` is not specified, `stages` returns a list of character vectors containing the stages associated to each variable in the model (that is `object$stages`).

---

stages_bhc	<i>Backward hill-climbing</i>
------------	-------------------------------

---

**Description**

Greedy search of staged event trees with iterative joining of stages.

**Usage**

```
stages_bhc(
  object,
  score = function(x) { return(-BIC(x)) },
  max_iter = Inf,
  scope = NULL,
  ignore = object$name_unobserved,
  trace = 0
)
```

**Arguments**

<code>object</code>	an object of class <code>sevt</code> with fitted probabilities and data, as returned by <code>full</code> or <code>sevt_fit</code> .
<code>score</code>	the score function to be maximized.
<code>max_iter</code>	the maximum number of iterations per variable.
<code>scope</code>	names of variables that should be considered for the optimization.
<code>ignore</code>	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in <code>object\$name_unobserved</code> .
<code>trace</code>	if $>0$ increasingly amount of info is printed (via message).

**Details**

For each variable the algorithm tries to join stages and moves to the best model that increases the score. When no increase is possible it moves to the next variable.

**Value**

The final staged event tree obtained.

**Examples**

```
DD <- generate_xor_dataset(n = 4, N = 100)
model <- stages_bhc(full(DD), trace = 2)
summary(model)
```



---

stages_bhcr	<i>Backward random hill-climbing</i>
-------------	--------------------------------------

---

### Description

Randomly try to join stages. This is a pretty-useless function, used for comparisons.

### Usage

```
stages_bhcr(  
  object,  
  score = function(x) { return(-BIC(x)) },  
  max_iter = 100,  
  trace = 0  
)
```

### Arguments

object	an object of class sevt.
score	the score function to be maximized.
max_iter	the maximum number of iteration.
trace	if >0 increasingly amount of info is printed (via message).

### Details

At each iteration a variable and two of its stages are randomly selected. If joining the stages increases the score, the model is updated. The procedure is repeated until the number of iterations reaches max\_iter.

### Value

an object of class sevt.

### Examples

```
DD <- generate_xor_dataset(n = 4, N = 100)  
model <- stages_bhcr(full(DD), trace = 2)  
summary(model)
```

---

stages\_bj                      *Backward joining of stages*

---

**Description**

Join stages from more complex to simpler models using a distance and a threshold value.

**Usage**

```
stages_bj(
  object = NULL,
  distance = "kullback",
  thr = 0.1,
  scope = NULL,
  ignore = object$name_unobserved,
  trace = 0
)
```

**Arguments**

object	an object of class <code>sevt</code> with fitted probabilities and data, as returned by <code>full</code> or <code>sevt_fit</code> .
distance	character, see details.
thr	the threshold for joining stages
scope	names of variables that should be considered for the optimization.
ignore	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in <code>object\$name_unobserved</code> .
trace	if >0 increasingly amount of info is printed (via message).

**Details**

For each variable in the model stages are joined iteratively. At each iteration the two stages with minimum distance are selected and joined if their distance is less than `thr`.

Available distances are: `manhattan` (`manhattan`), `euclidean` (`euclidean`), `Renyi divergence` (`renyi`), `Kullback-Liebler` (`kullback`), `total-variation` (`totvar`), `squared Hellinger` (`hellinger`), `Bhattacharyya` (`bhatt`), `Chan-Darwiche` (`chandarw`). See also [probdist](#).

**Value**

The final staged event tree obtained.

**Examples**

```
DD <- generate_xor_dataset(n = 5, N = 1000)
model <- stages_bj(full(DD, lambda = 1), trace = 2)
summary(model)
```

---

stages_fbhc	<i>Fast backward hill-climbing</i>
-------------	------------------------------------

---

### Description

Greedy search of staged event trees with iterative joining of stages.

### Usage

```
stages_fbhc(
  object = NULL,
  score = function(x) { return(-BIC(x)) },
  max_iter = Inf,
  scope = NULL,
  ignore = object$name_unobserved,
  trace = 0
)
```

### Arguments

object	an object of class <code>sevt</code> with fitted probabilities and data, as returned by <code>full</code> or <code>sevt_fit</code> .
score	the score function to be maximized.
max_iter	the maximum number of iteration.
scope	names of variables that should be considered for the optimization.
ignore	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in <code>object\$name_unobserved</code> .
trace	if $>0$ increasingly amount of info is printed (via message).

### Details

For each variable the algorithm tries to join stages and moves to the first model that increases the score. When no increase is possible it moves to the next variable.

### Value

The final staged event tree obtained.

### Examples

```
DD <- generate_xor_dataset(n = 5, N = 100)
model <- stages_fbhc(full(DD), trace = 2)
summary(model)
```

---

 stages\_hc

*Hill-climbing*


---

**Description**

Greedy search of staged event trees with iterative moving of nodes between stages.

**Usage**

```

stages_hc(
  object,
  score = function(x) { return(-BIC(x)) },
  max_iter = Inf,
  scope = NULL,
  ignore = object$name_unobserved,
  trace = 0
)

```

**Arguments**

object	an object of class <code>sevt</code> with fitted probabilities and data, as returned by <code>full</code> or <code>sevt_fit</code> .
score	the score function to be maximized.
max_iter	the maximum number of iterations per variable.
scope	names of variables that should be considered for the optimization
ignore	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in <code>object\$name_unobserved</code> .
trace	if >0 increasingly amount of info is printed (via message).

**Details**

For each variable node-moves that best increases the score are performed until no increase is possible. A node-move is either changing the stage associate to a node or move the node to a new stage.

The `ignore` argument can be used to specify stages that should not be affected during the search, that is left untouched. This is useful for preserving structural zeroes and to speed-up computations.

**Value**

The final staged event tree obtained.

**Examples**

```

start <- indep(PhDArticles[,1:5], join_unobserved = TRUE)
model <- stages_hc(start)

```

---

`stages_hclust`*Learn a staged tree with hierarchical clustering*

---

### Description

Build a stage event tree with  $k$  stages for each variable by clustering stage probabilities with hierarchical clustering.

### Usage

```
stages_hclust(  
  object,  
  distance = "totvar",  
  k = length(object$tree[[1]]),  
  method = "complete",  
  ignore = object$name_unobserved,  
  limit = length(object$tree),  
  scope = NULL  
)
```

### Arguments

<code>object</code>	an object of class <code>sevt</code> with fitted probabilities and data, as returned by <code>full</code> or <code>sevt_fit</code> .
<code>distance</code>	character, the distance measure to be used, either a possible method for <code>dist</code> or one of the following: "totvar", "hellinger".
<code>k</code>	integer or (named) vector: number of clusters, that is stages per variable. Values will be recycled if needed.
<code>method</code>	the agglomeration method to be used in <code>hclust</code> .
<code>ignore</code>	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in <code>object\$name_unobserved</code> .
<code>limit</code>	the maximum number of variables to consider.
<code>scope</code>	names of the variables to consider.

### Details

`hclust_sevt` performs hierarchical clustering of the initial stage probabilities in `object` and it aggregates them into the specified number of stages ( $k$ ). A different number of stages for the different variables in the model can be specified by supplying a (named) vector via the argument `k`.

### Value

A staged event tree object.

**Examples**

```
data("Titanic")
model <- stages_hclust(full(Titanic, join_unobserved = TRUE, lambda = 1), k = 2)
summary(model)
```

---

stages\_kmeans

*Learn a staged tree with k-means clustering*


---

**Description**

Build a stage event tree with  $k$  stages for each variable by clustering (transformed) probabilities with  $k$ -means.

**Usage**

```
stages_kmeans(
  object,
  k = length(object$tree[[1]]),
  algorithm = "Hartigan-Wong",
  transform = sqrt,
  ignore = object$name_unobserved,
  limit = length(object$tree),
  scope = NULL,
  nstart = 1
)
```

**Arguments**

object	an object of class <code>sevt</code> with fitted probabilities and data, as returned by <code>full</code> or <code>sevt_fit</code> .
k	integer or (named) vector: number of clusters, that is stages per variable. Values will be recycled if needed.
algorithm	character: as in <a href="#">kmeans</a> .
transform	function applied to the probabilities before clustering.
ignore	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in <code>object\$name_unobserved</code> .
limit	the maximum number of variables to consider.
scope	names of the variables to consider.
nstart	as in <a href="#">kmeans</a>

**Details**

`kmenas_sevt` performs  $k$ -means clustering to aggregate the stage probabilities of the initial staged tree object. Different values for  $k$  can be specified by supplying a (named) vector to `k`. [kmeans](#) from the `stats` package is used internally and arguments `algorithm` and `nstart` refer to the same arguments as [kmeans](#).

**Value**

A staged event tree.

**Examples**

```
data("Titanic")
model <- stages_kmeans(full(Titanic, join_unobserved = TRUE, lambda = 1), k = 2)
summary(model)
```

---

stndnaming

*Standard renaming of stages*


---

**Description**

Rename all stages in a staged event tree.

**Usage**

```
stndnaming(
  object,
  uniq = FALSE,
  prefix = FALSE,
  ignore = object$name_unobserved
)
```

**Arguments**

object	an object of class <code>sevt</code> .
uniq	logical, if stage numbers should be unique over all tree.
prefix	logical, if stage names should be prefixed with variable name.
ignore	vector of stages which will be ignored and left untouched, by default the name of the unobserved stages stored in <code>object\$name_unobserved</code> .

**Value**

a staged event tree object with stages named with consecutive integers.

**Examples**

```
model <- stages_fbhc(full(PhDArticles, join_unobserved = TRUE))
model$stages
model1 <- stndnaming(model)
model1$stages

### unique stage names in all tree
model2 <- stndnaming(model, uniq = TRUE)
model2$stages
```

```
### prefix stage names with variable name
model3 <- stndnaming(model, prefix = TRUE)
model3$stages

### manually select stage names left untouched
model4 <- stndnaming(model, ignore = c("2", "6"), prefix = TRUE)
model4$stages
```

---

subtree	<i>Extract subtree</i>
---------	------------------------

---

### Description

Extract subtree

### Usage

```
subtree(object, path)
```

### Arguments

object	an object of class <code>sevt</code> .
path	the path from root after which extract the subtree.

### Details

Returns the subtree of the staged event tree, starting from path.

### Value

A staged event tree object corresponding to the subtree.

### Examples

```
DD <- generate_random_dataset(4, 100)
model <- sevt(DD, full = TRUE)
plot(model)
model1 <- subtree(model, path = c("-1", "1"))
plot(model1)
```



---

summary.sevt	<i>Summarizing staged event trees</i>
--------------	---------------------------------------

---

**Description**

Summary method for class sevt.

**Usage**

```
## S3 method for class 'sevt'
summary(object, ...)

## S3 method for class 'summary.sevt'
print(x, max = 10, ...)
```

**Arguments**

object	an object of class sevt.
...	arguments for compatibility.
x	an object of class summary.sevt.
max	the maximum number of variables for which information is printed.

**Details**

Print model information and summary of stages.

**Value**

An object of class summary.sevt for which a print method exist.

**Examples**

```
model <- stages_fbhc(full(PhDArticles, lambda = 1))
summary(model)
```

---

text.sevt	<i>Add text to a staged event tree plot</i>
-----------	---

---

**Description**

Add text to a staged event tree plot

**Usage**

```
## S3 method for class 'sevt'
text(x, y = ylim[1], limit = 10, xlim = c(0, 1), ylim = c(0, 1), ...)
```

**Arguments**

<code>x</code>	An object of class <code>sevt</code> .
<code>y</code>	the position of the labels.
<code>limit</code>	maximum number of variables plotted.
<code>xlim</code>	graphical parameter.
<code>ylim</code>	graphical parameter.
<code>...</code>	additional parameters passed to <a href="#">text</a> .

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